

Acknowledgements



James Fraser Nevan Krogan

Paul Adams John Tainer Greg Hura Nick Sauter

Pavel Afonine Tom Terwilliger Nigel Moriarty, Dorothee Liebschner

Aina Cohen

UCSF LBNL SLAC

ALS 8.3.1: TomAlberTron

NIH NIGMS R01 GM124149 (Holton)

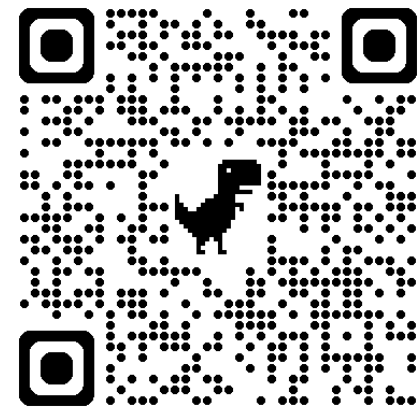
NIH NIAID P50 AI150476 (Krogan)

NIH NIGMS P30 GM124169 (Adams)

DOE-BER IDAT (Hura)

NIH NIGMS P30 GM133894 (Hodgson)

Why is a beamline guy doing refinement things?



Because: the future of crystallography has alternate conformations

✓ Single-conf models

✓ poor resolution

✓ Low signal/noise

✓ Phase Problem

☐ Dynamics?

☐ Mechanism?

☐ Small signal?

☐ Overlapping states?

Map Noise:

via Parseval's Theorem

$$\frac{\rho}{\sigma(\rho)} \approx \frac{e^-}{7R}$$

e^-

number of electrons in peak

7

number of electrons in typical atom

R

R_{iso} or R_{free}

ρ

electron density peak

σ

rms deviation expected

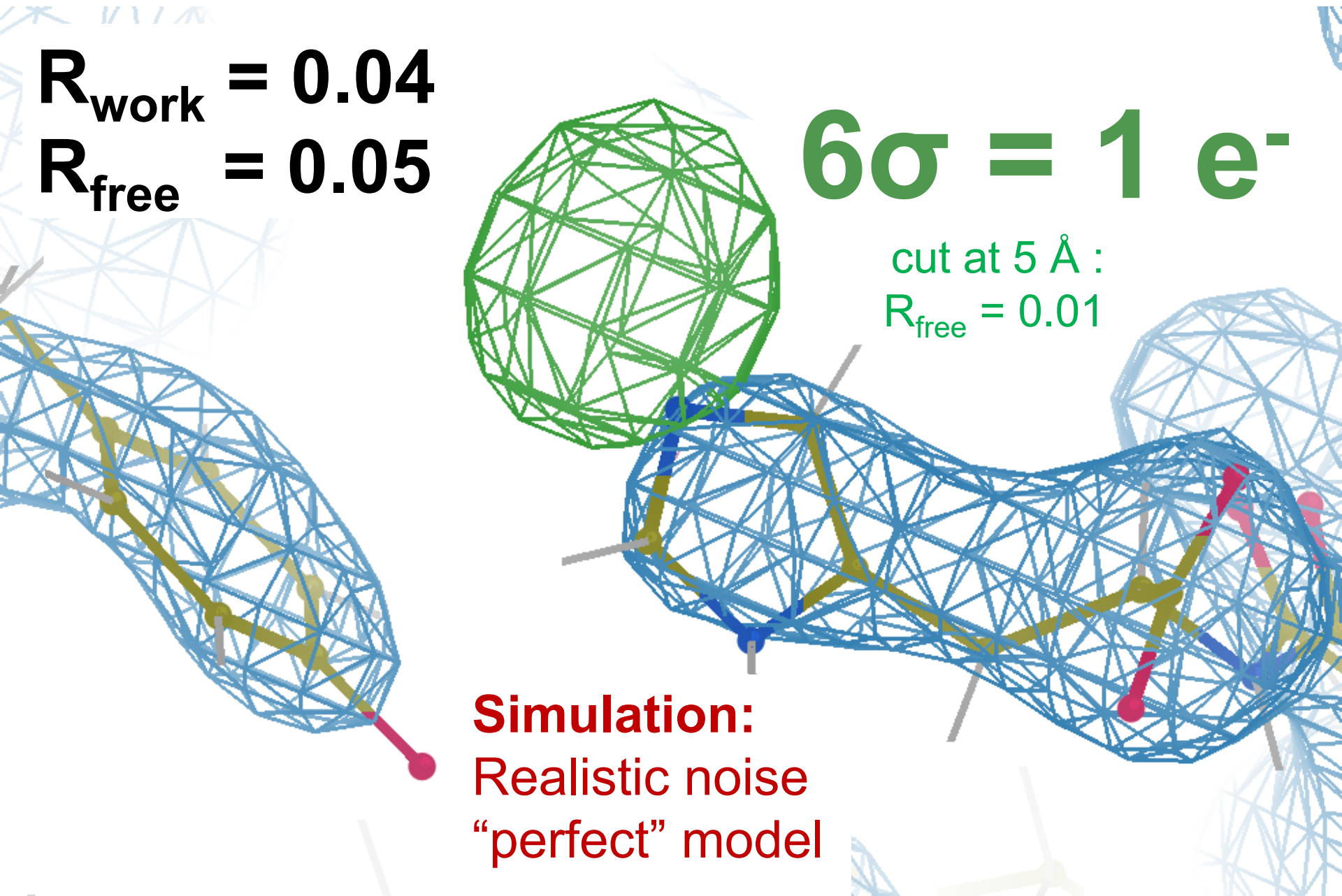
Hydrogen: visible at 3.5 Å resolution!

$$R_{\text{work}} = 0.04$$

$$R_{\text{free}} = 0.05$$

$$6\sigma = 1 e^-$$

cut at 5 Å :
 $R_{\text{free}} = 0.01$



Simulation:
Realistic noise
“perfect” model

R_{work} : 0.0823
 R_{free} : 0.1106
bond: 0.014 Å
angle: 1.92°

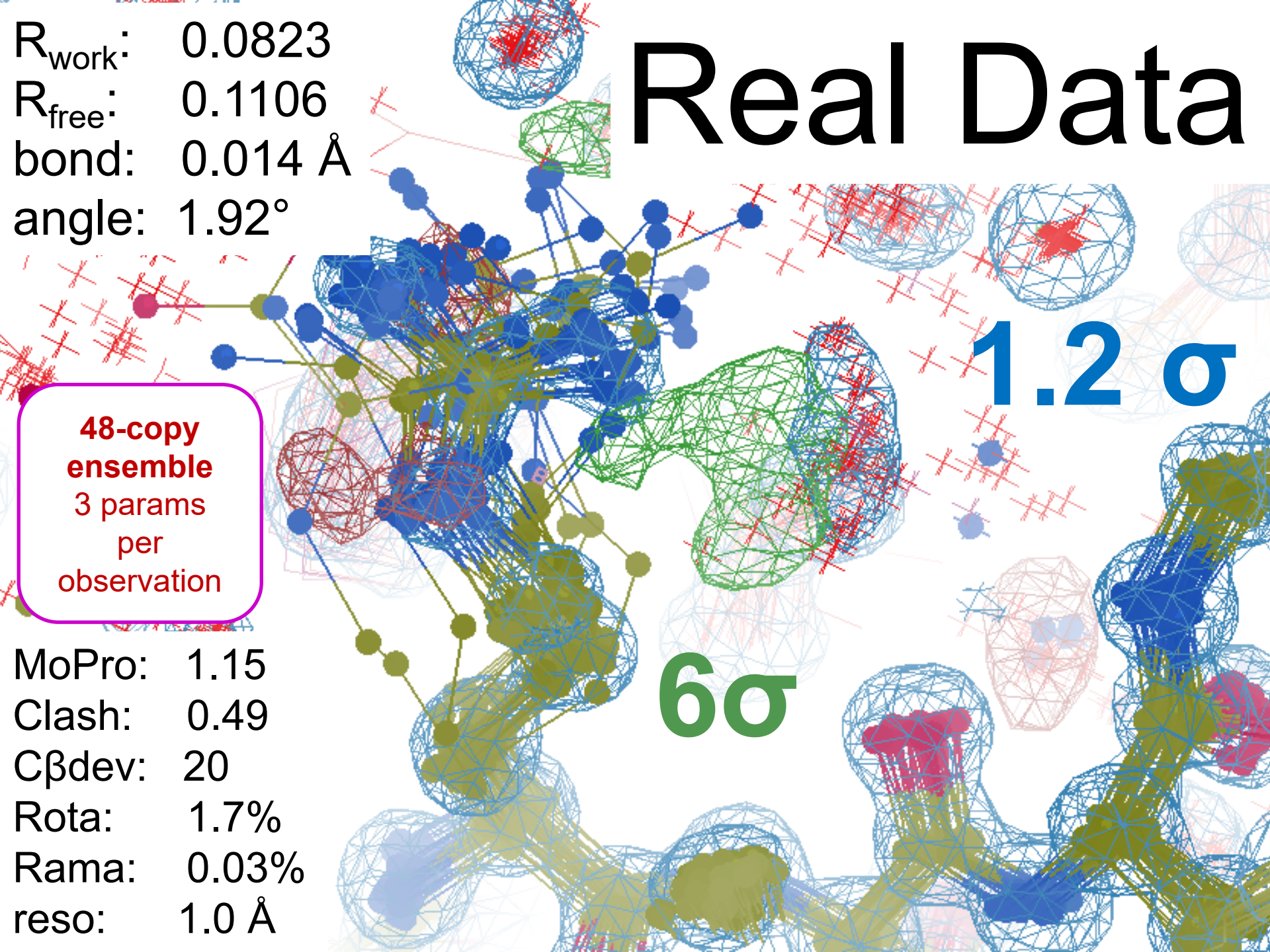
Real Data

1.2 σ

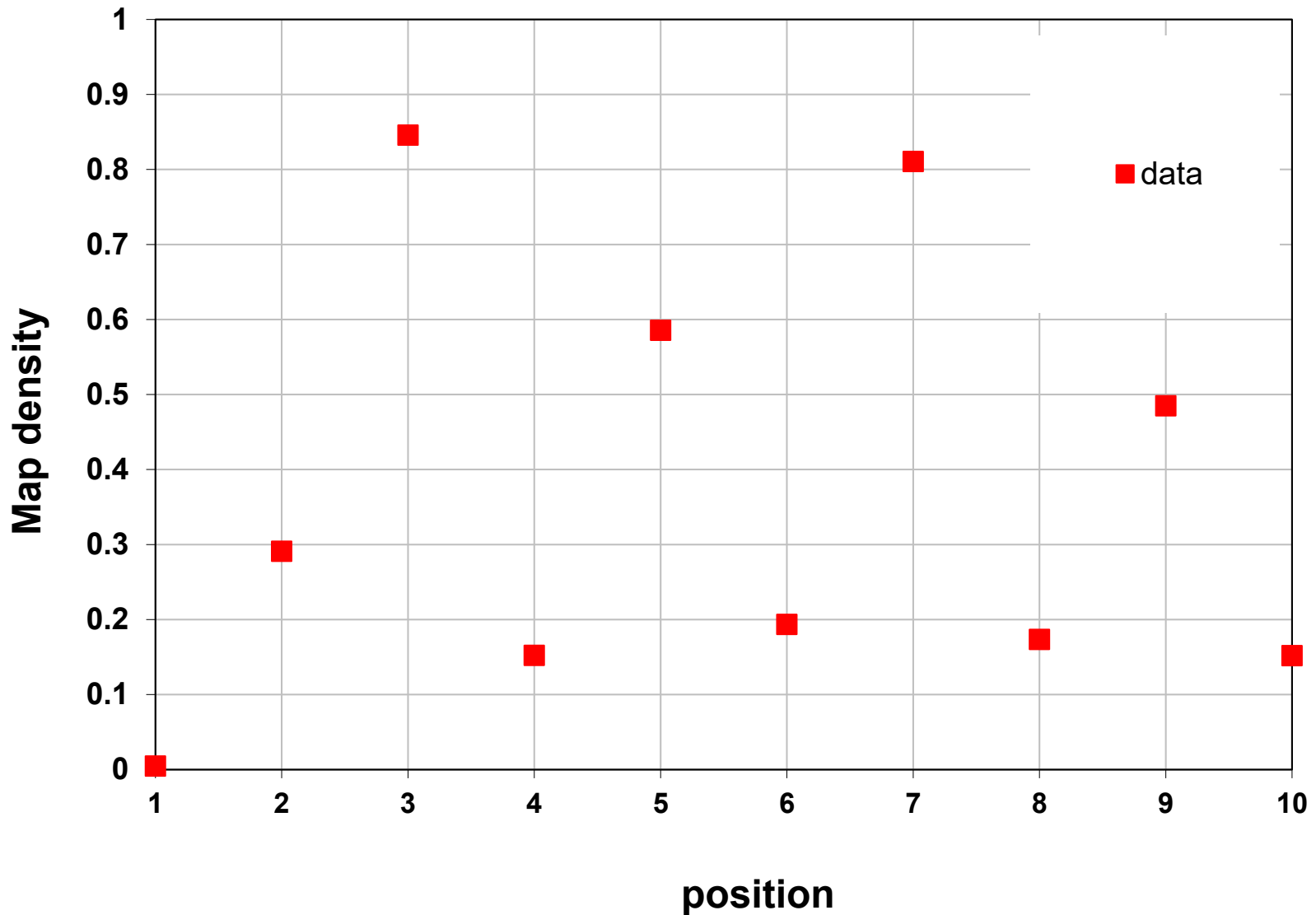
48-copy
ensemble
3 params
per
observation

6 σ

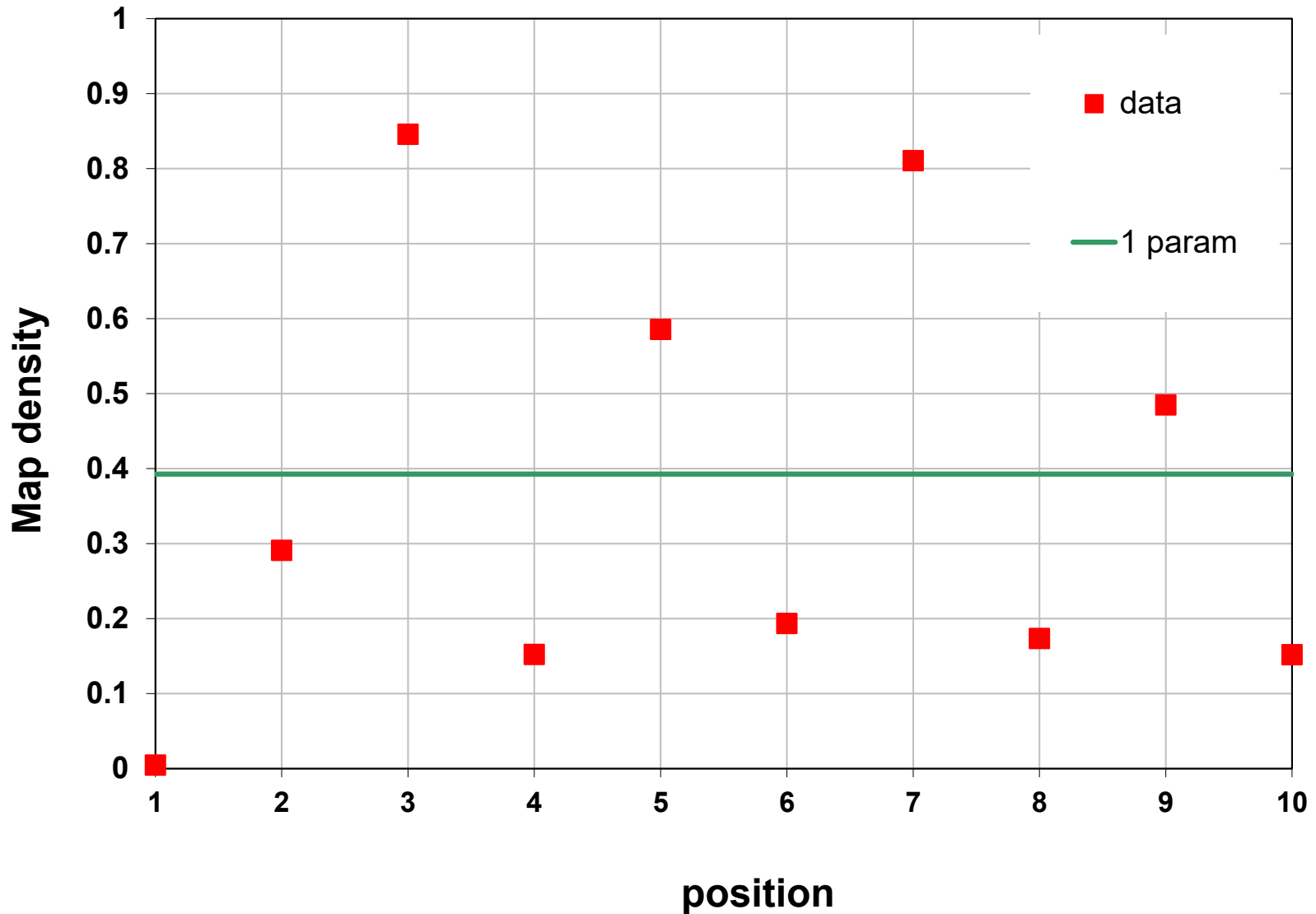
MoPro: 1.15
Clash: 0.49
C β dev: 20
Rota: 1.7%
Rama: 0.03%
reso: 1.0 Å



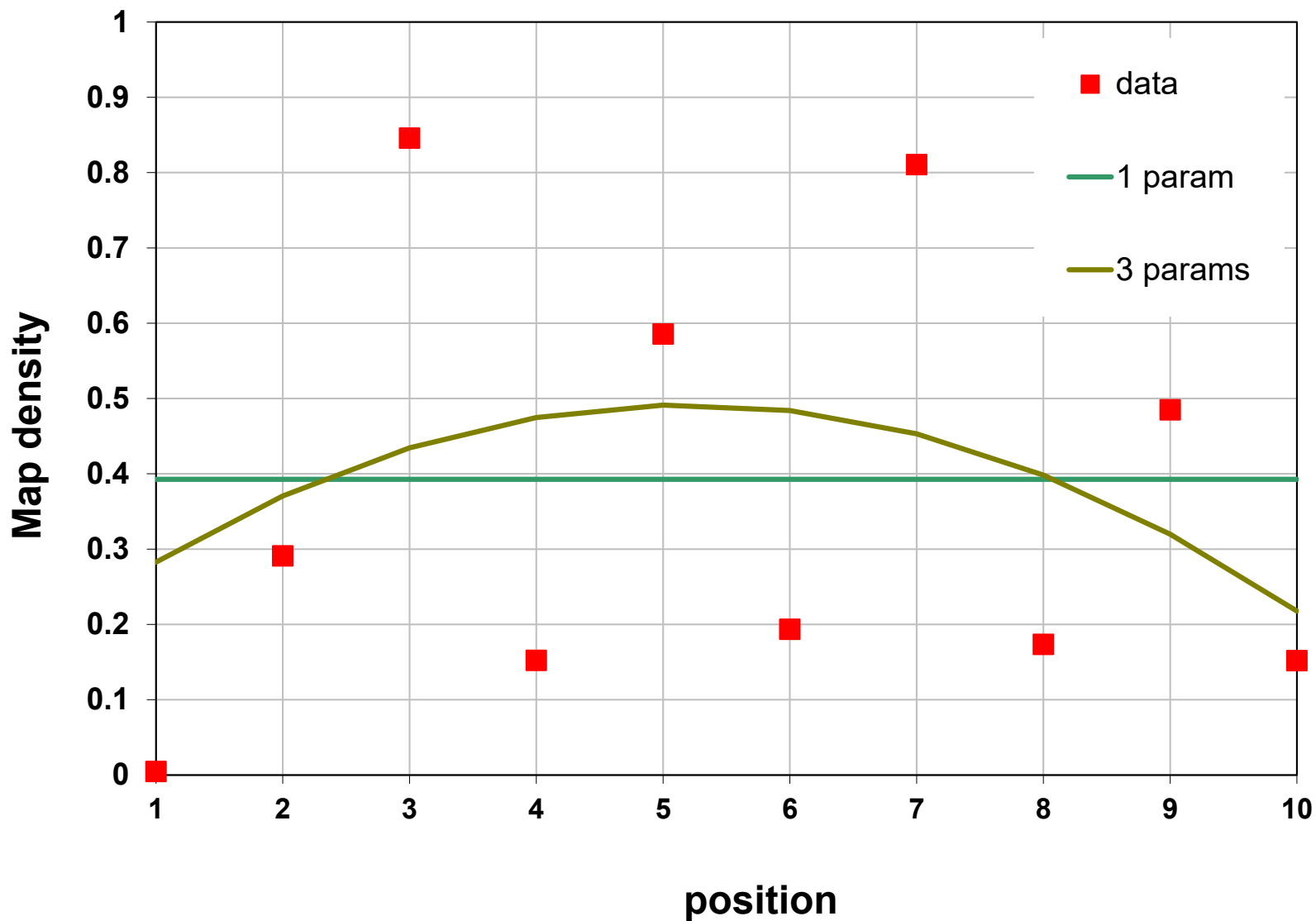
Over-Fitting data



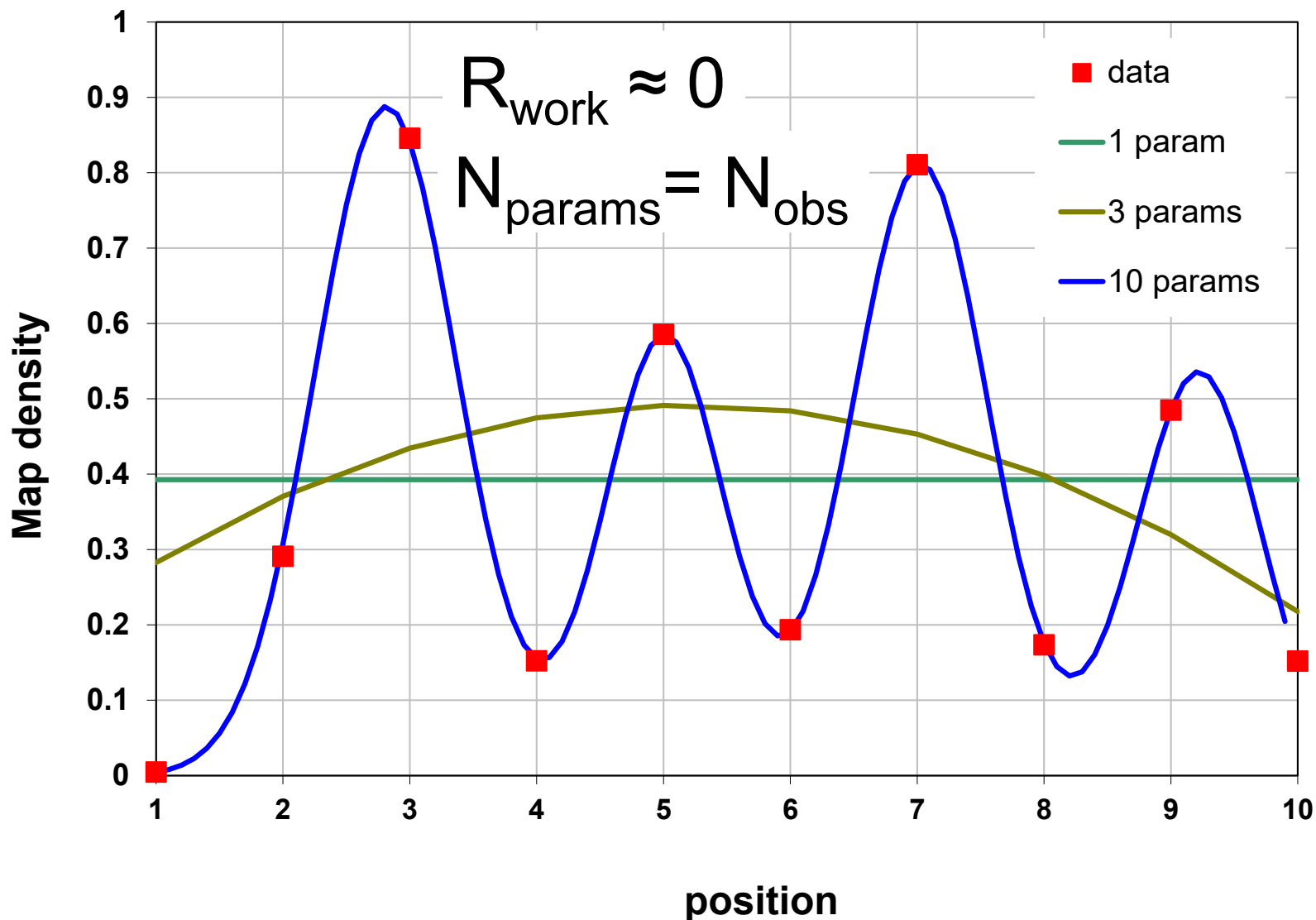
Over-Fitting data



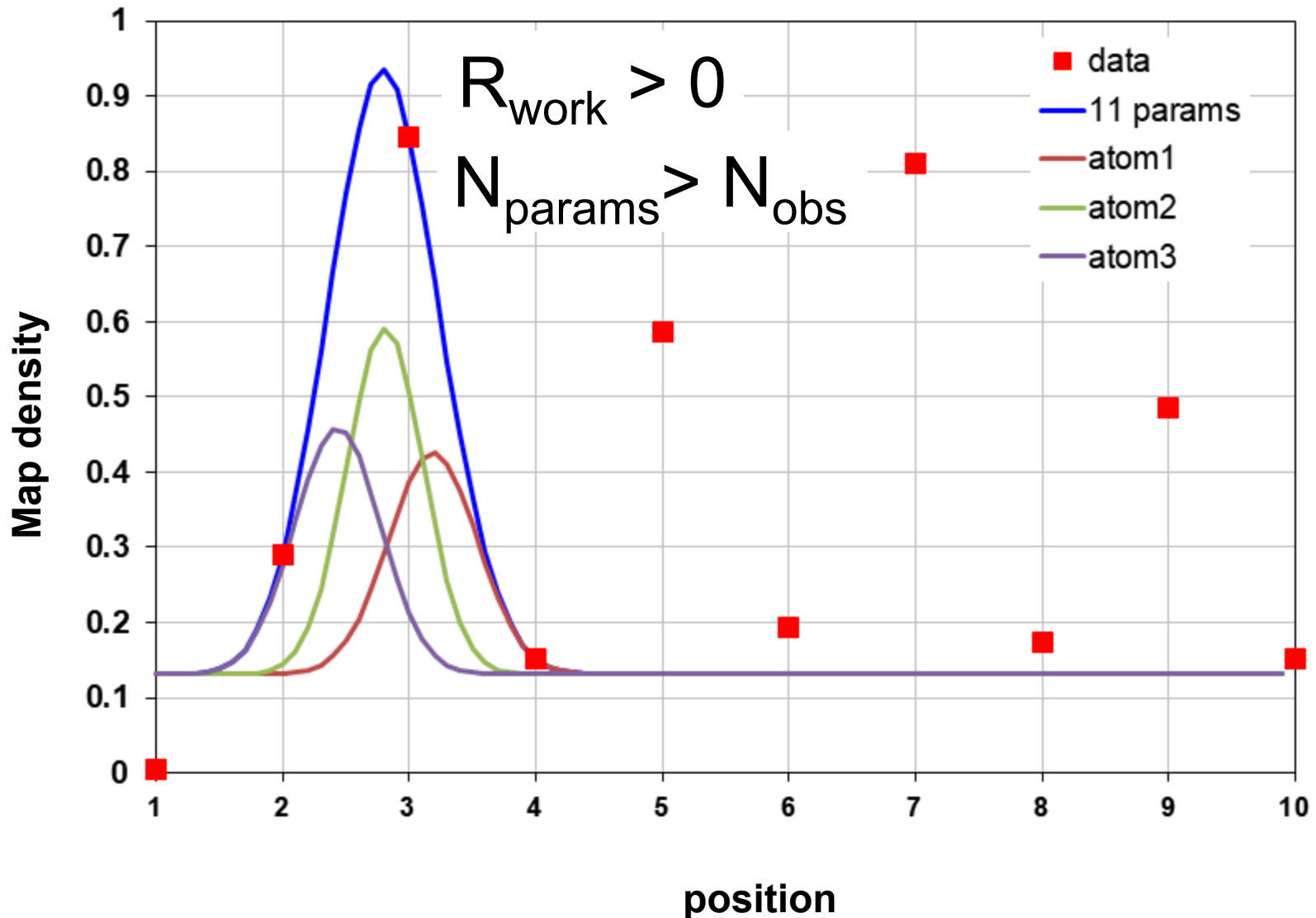
Over-Fitting data



Over-Fitting data



Under-Fitting data



R_{work} : 0.0823

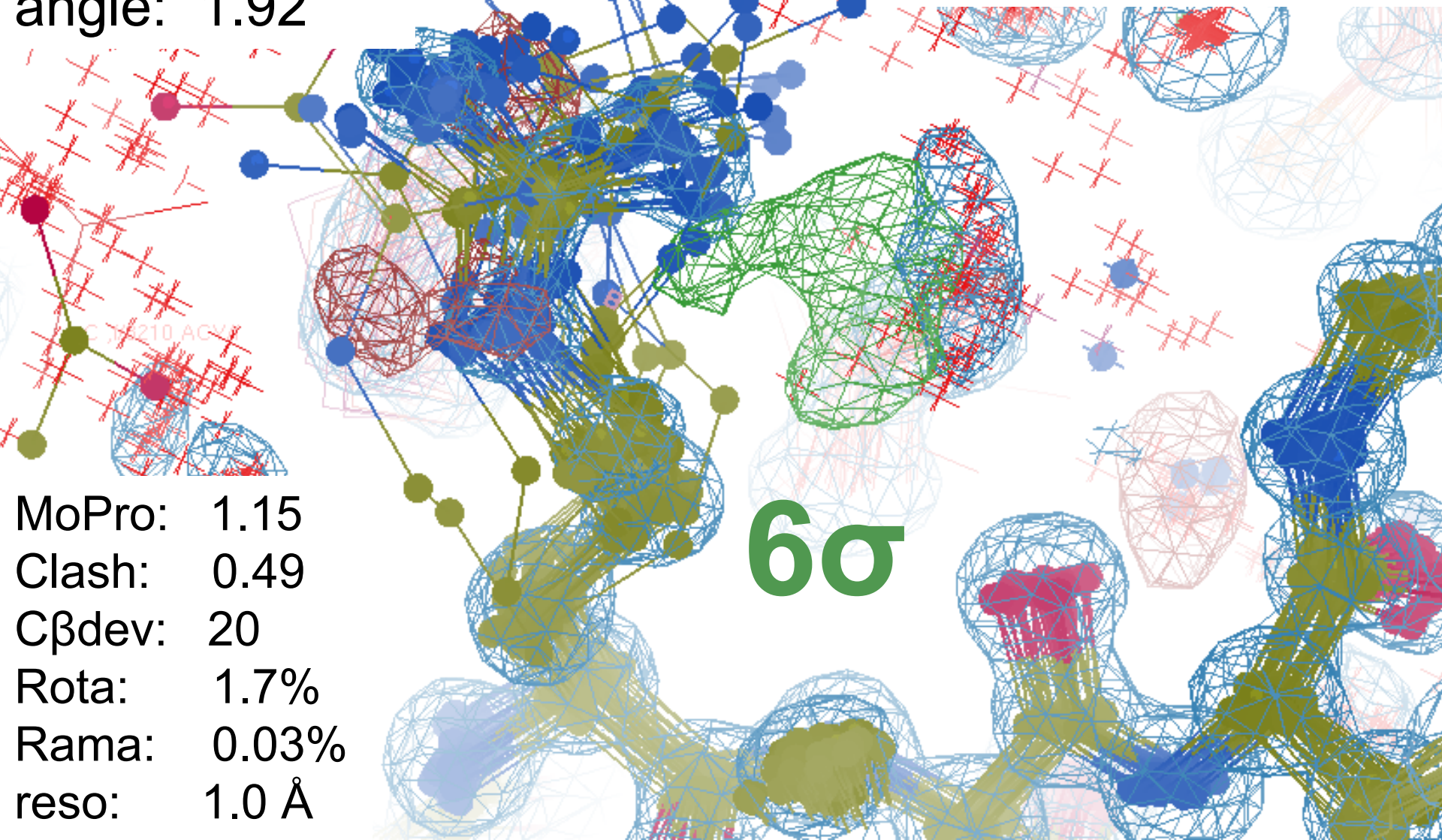
R_{free} : 0.1106

bond: 0.014 Å

angle: 1.92°

under-fitting:

$R_{\text{work}} > 0$



MoPro: 1.15

Clash: 0.49

Cβdev: 20

Rota: 1.7%

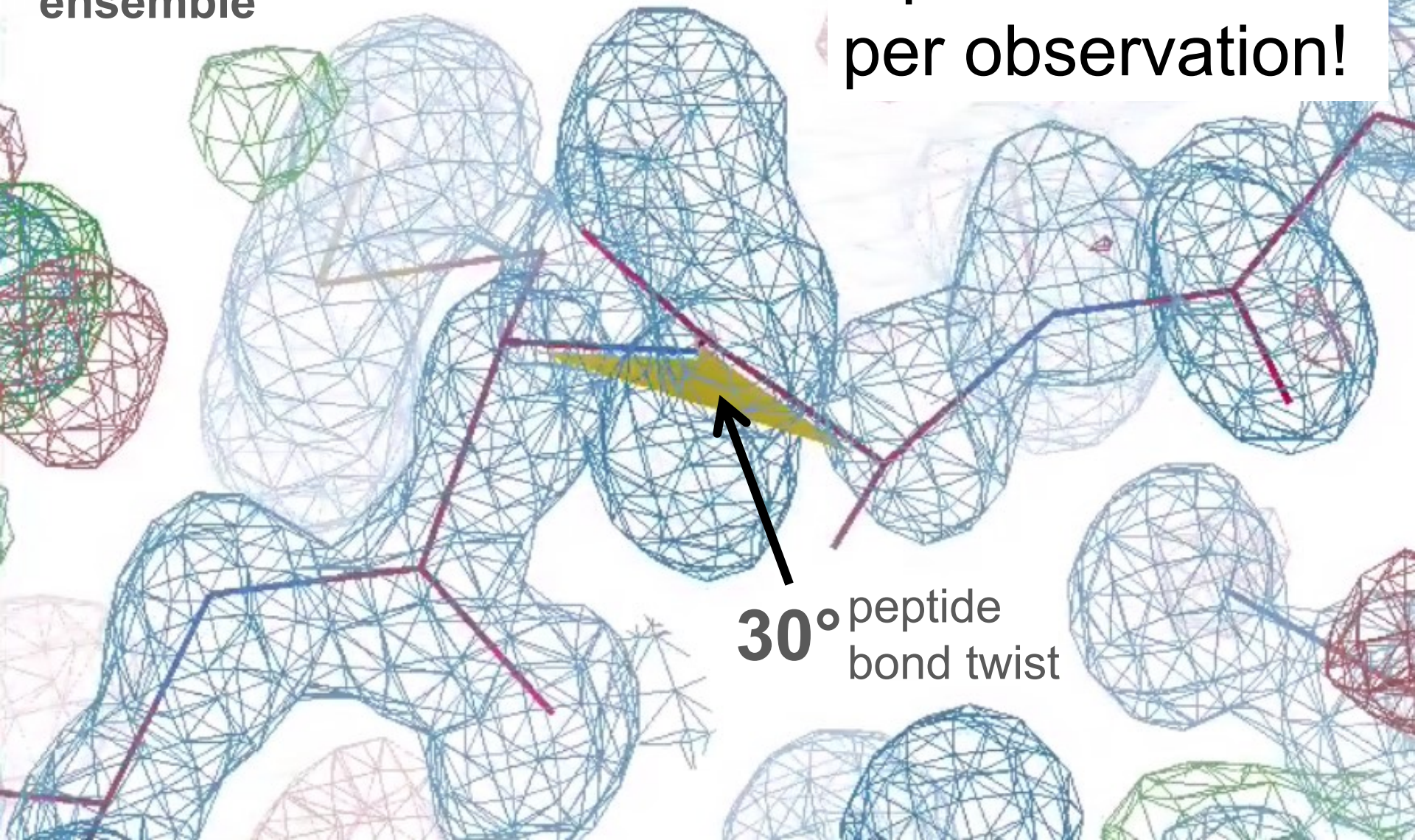
Rama: 0.03%

reso: 1.0 Å

What is holding it back?

1 member of 48-copy
ensemble

3 parameters
per observation!



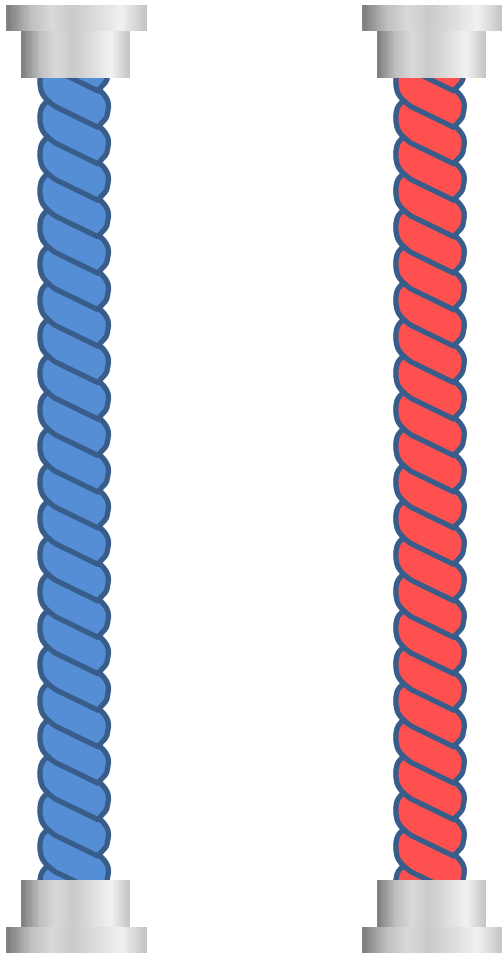
Why does ensemble refinement **suck**?

(3 parameters/observation and R_{work} still high!)

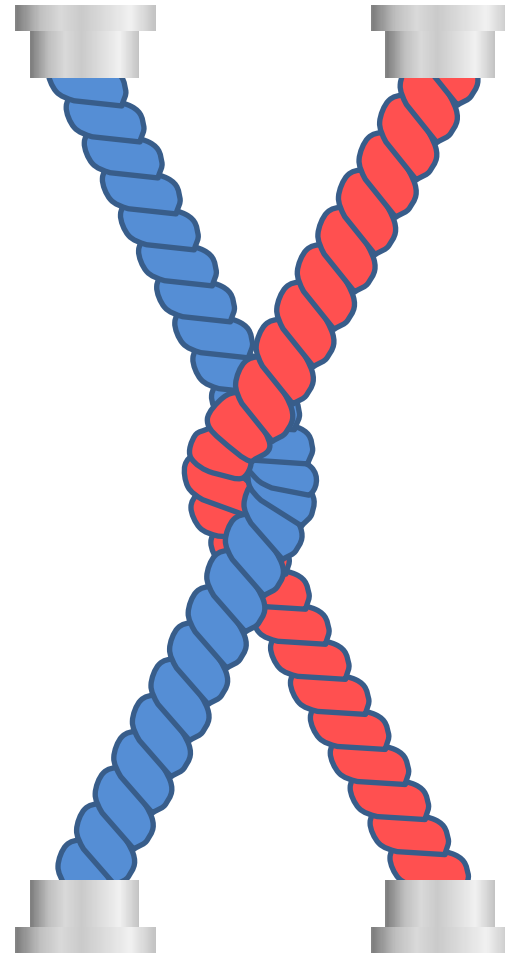
The chains are “tangled”

What do you mean, “tangled”?

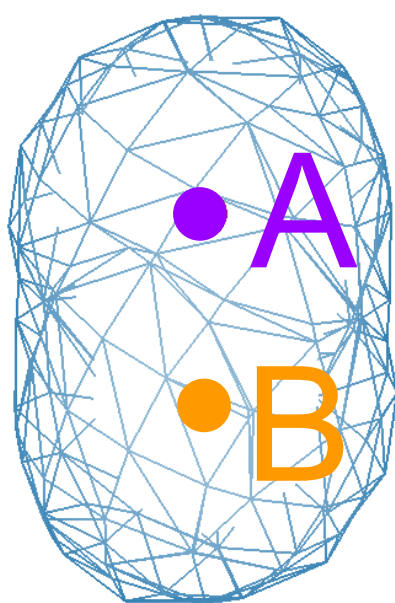
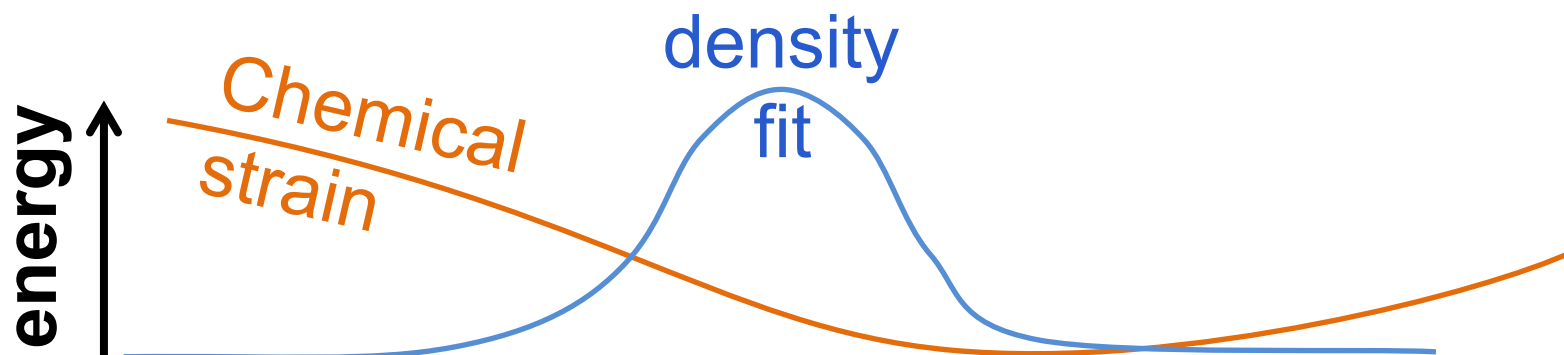
Ground Truth



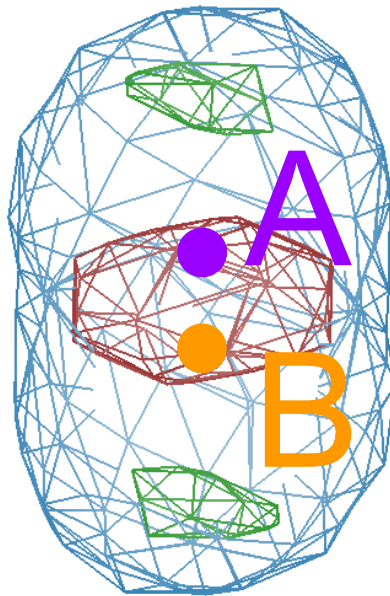
Local Minimum



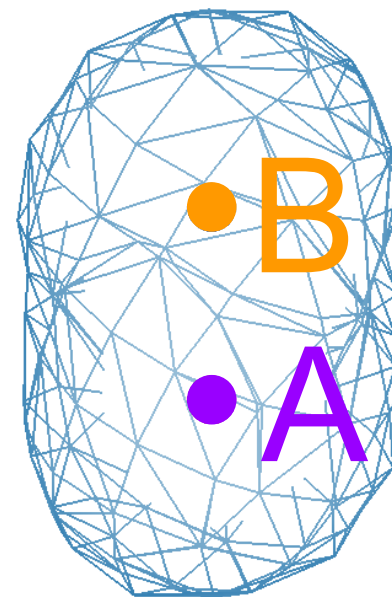
It takes two to tangle



tangled



barrier

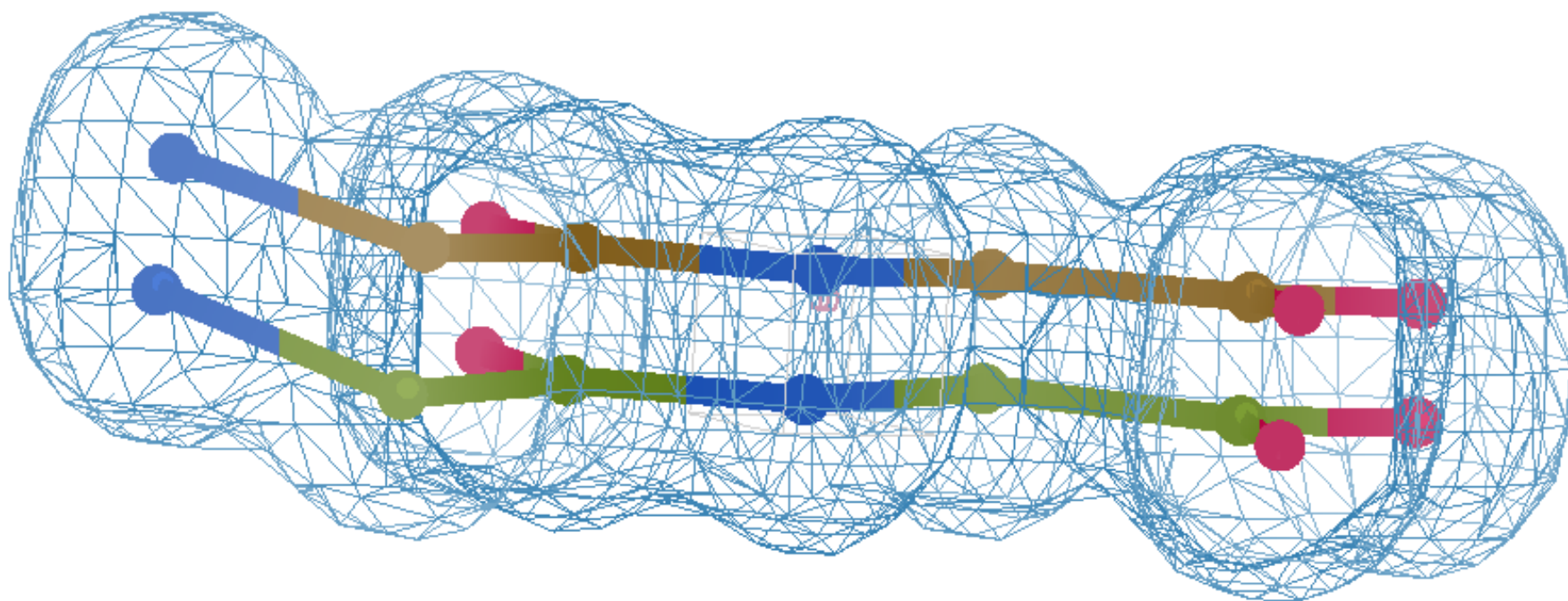
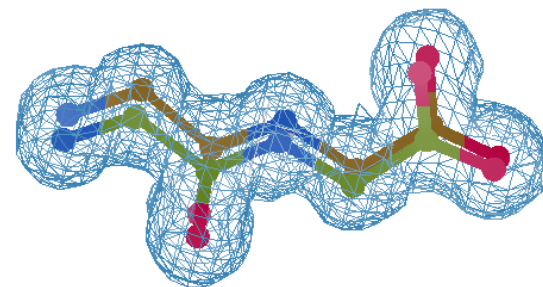


untangled

Refine from right answer

$R = 0.8\%$

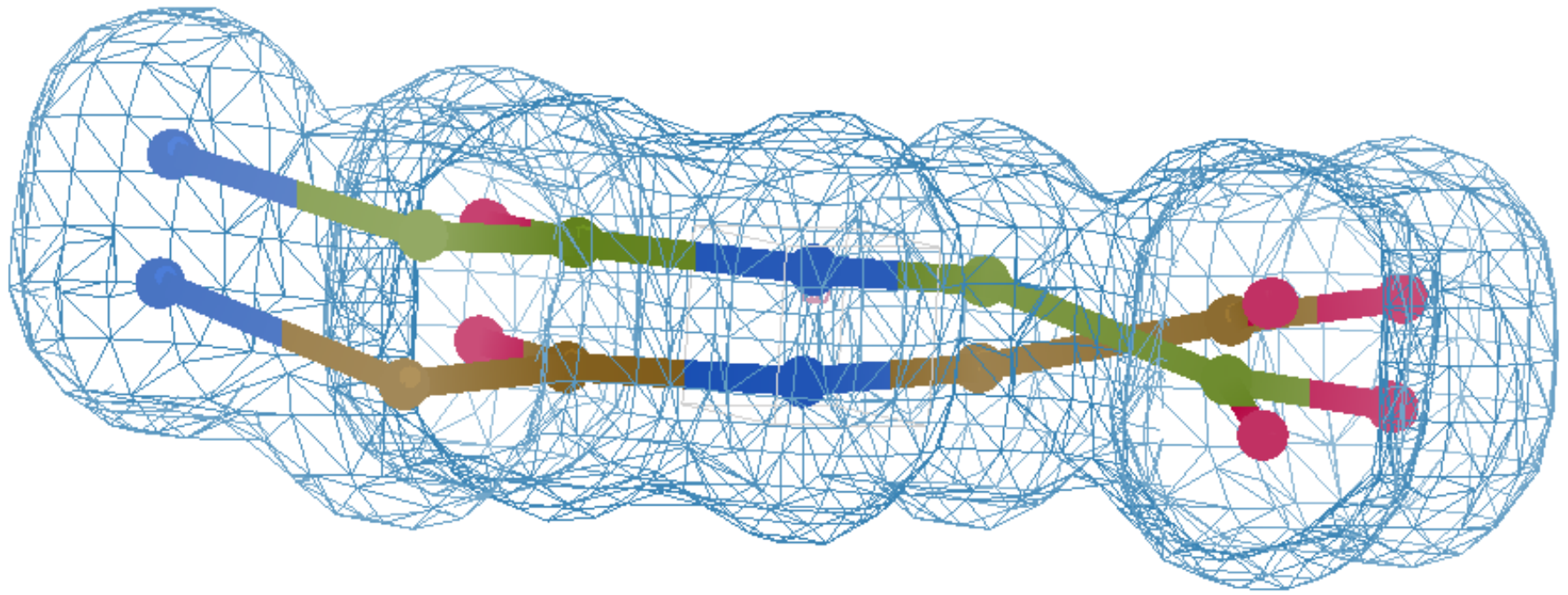
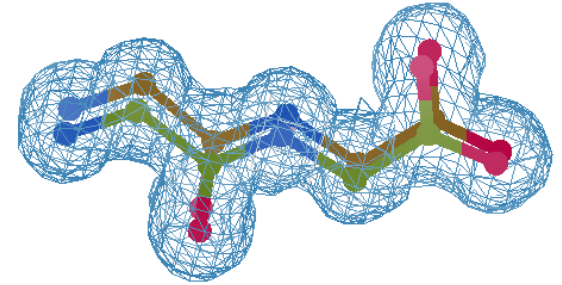
rms bond = 0.0002



Refine from wrong starting point

$R = 7.07\%$

rms bond = 0.001



UNTANGLE: sim-data Ground Truth

- As **simple** as possible:
 - 2 conformers
 - 50:50 occupancy
 - flat bulk solvent
 - no false outliers
- **Accessible**
 - 64 residues
 - 78 waters
 - phenix, refmac, shelxl
 - clear score
- Every chance of **success**
 - 1.0 Å reso
 - “one thing wrong”
 - Experimental error only
 - perfect phases

The UNTANGLE Challenge

best.pdb

refme.mtz

11) Build better than the best:

as-good or better wE, R_{free} as best.pdb

non-equivalent ensemble

\$1000

10) Recover best.pdb from refme.mtz

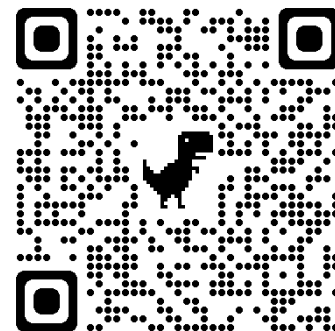
true phases, auto-building allowed

no cheating (don't use best.pdb as guide)

\$500

Prove: true ensemble is unique
and can be recovered

<https://github.com/jmholton/UnTangle>



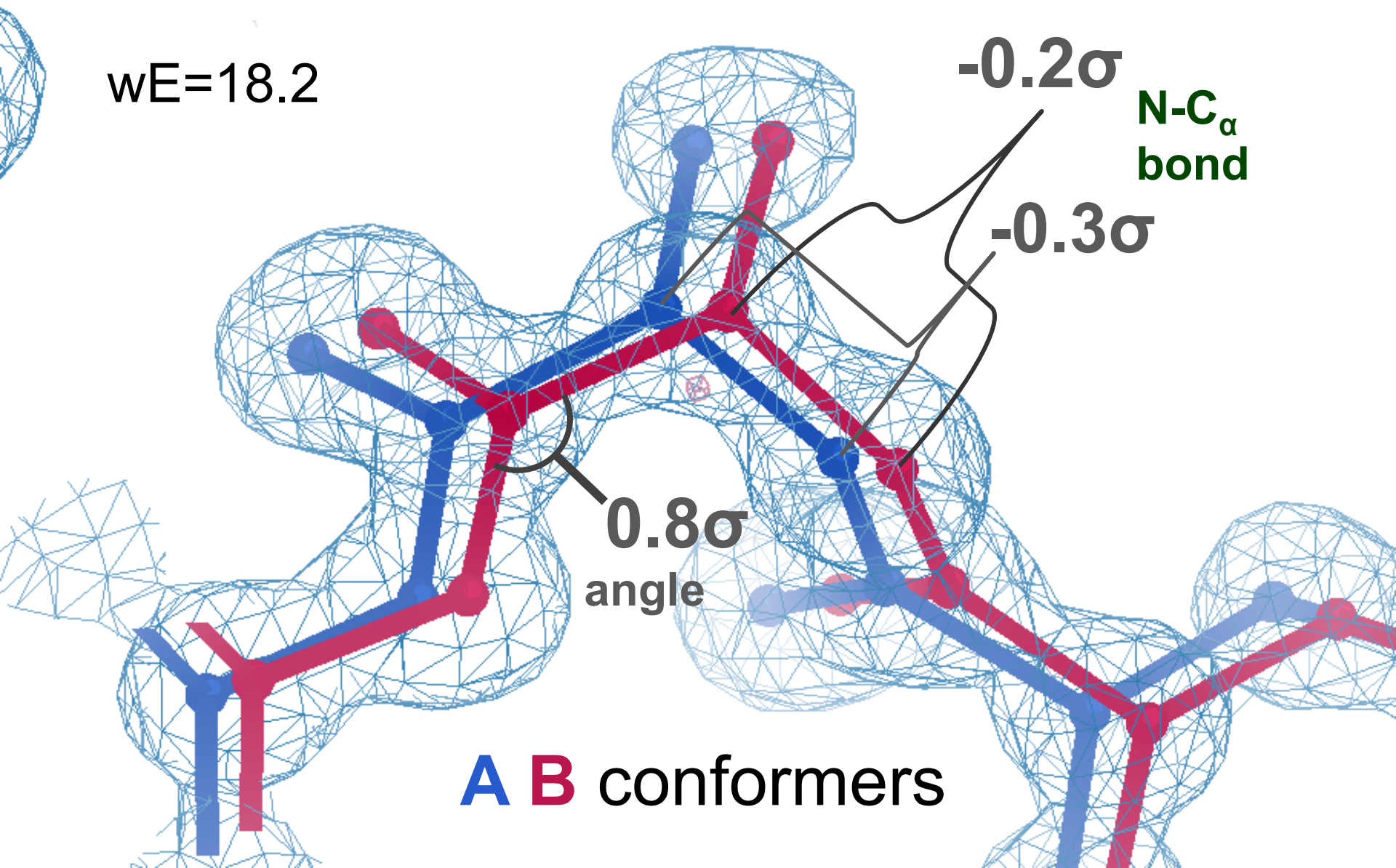
verified Score sheet

wE	R _{work}	R _{free}	method
185	20.6	21.4	Alphafold2
109.6	8.87	9.44	Phenix.ensemble_refine
97.3	8.84	9.27	qFit best
91.7	3.64	4.27	manual
80.5	4.31	4.75	lotswrong
65.2	6.35	6.93	Amber24
54.6	5.87	6.57	single conf w aniso B
33.5	2.94	3.32	One thing wrong: Ala39
23.5	2.95	3.31	One thing wrong: Val1
21.4	3.12	3.48	Rectified Simulated annealing
18.1	17.9	18.4	Phenix autobuild
18.2	2.79	3.14	best (ground truth)

Sim challenge data

Ala39

wE=18.2



N-C $_{\alpha}$
bond

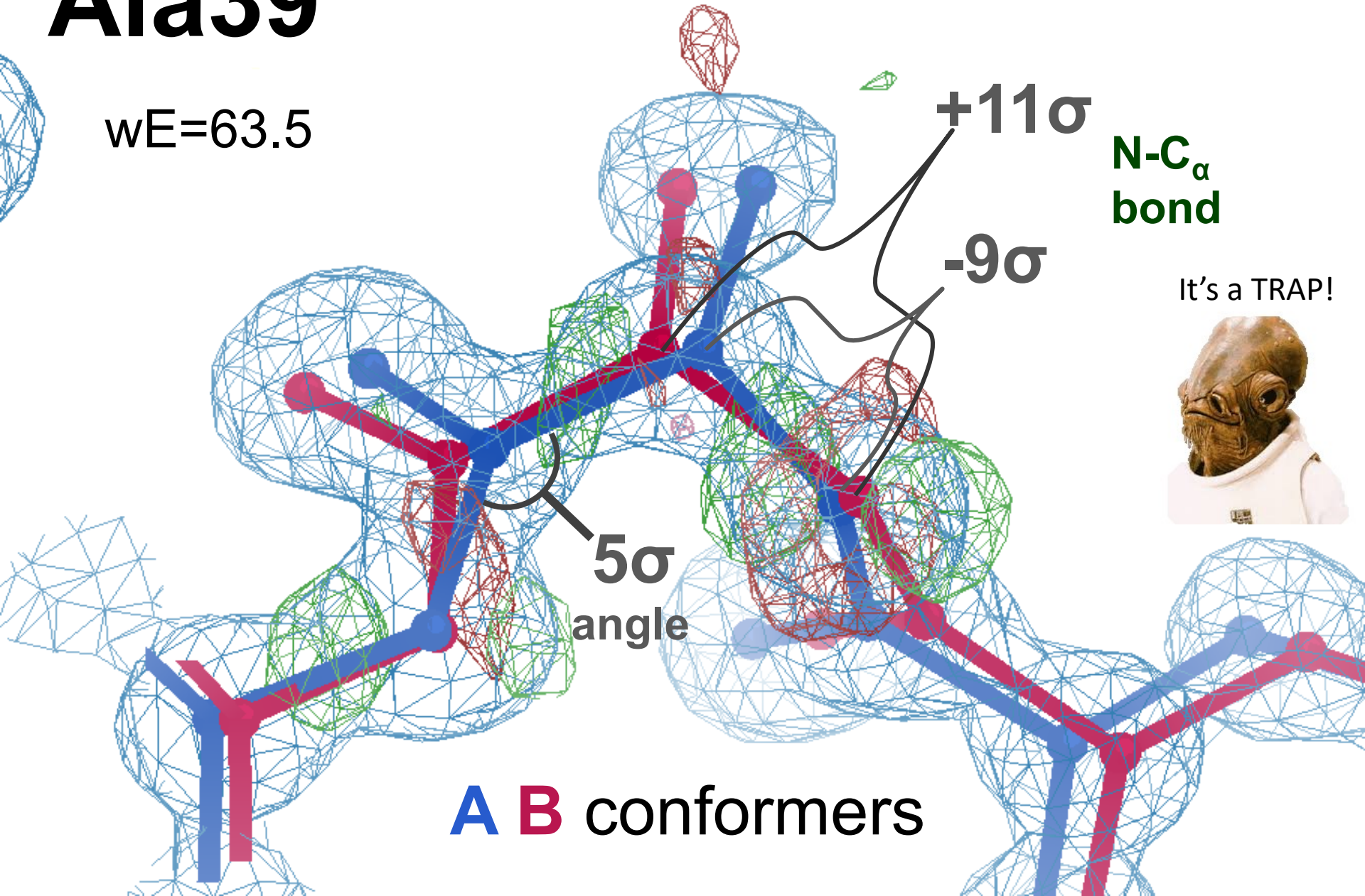
0.8σ
angle

A B conformers

Sim challenge data: "otw39"

Ala39

wE=63.5



It's a TRAP!

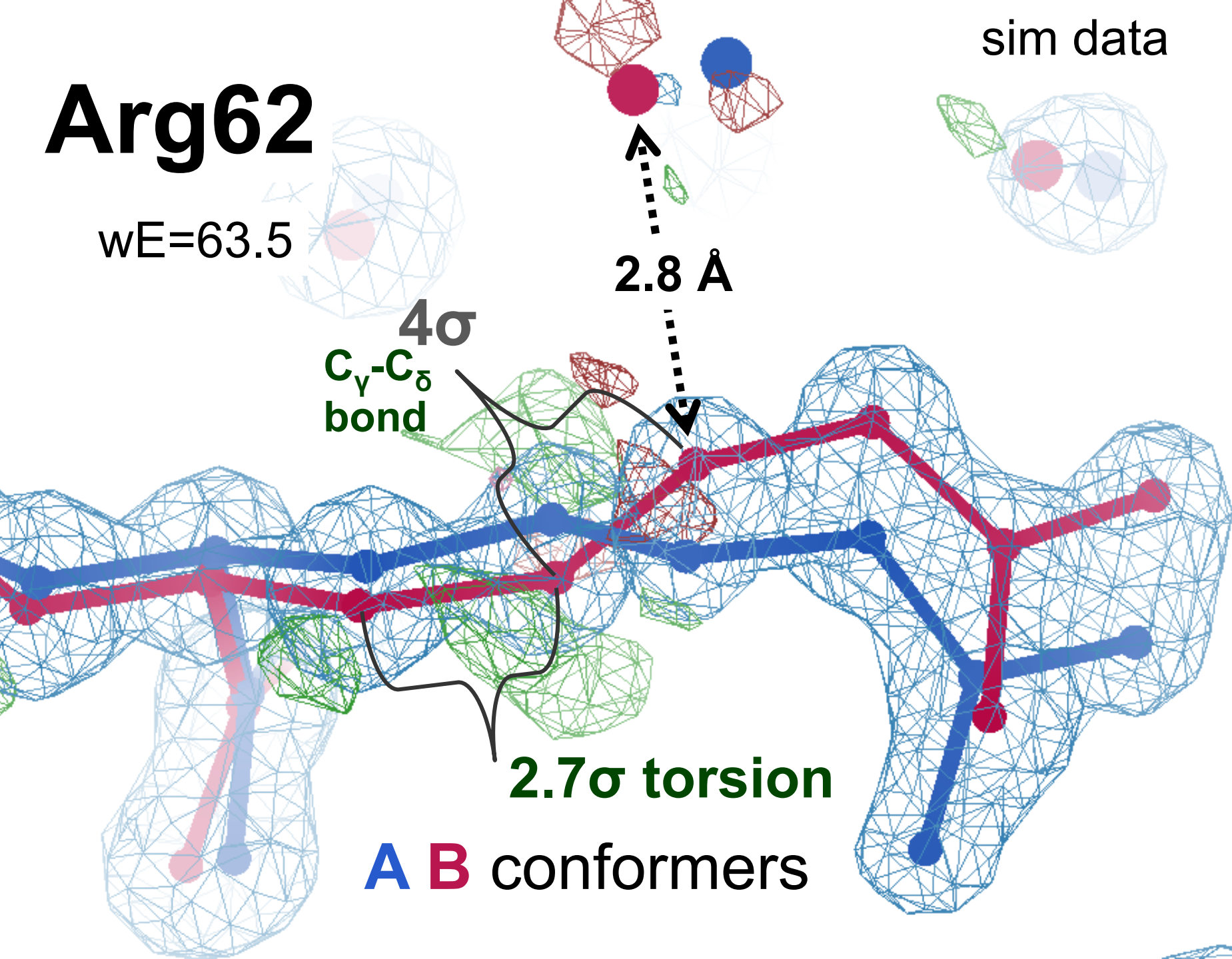


A B conformers

Arg62

wE=63.5

sim data



Arg62

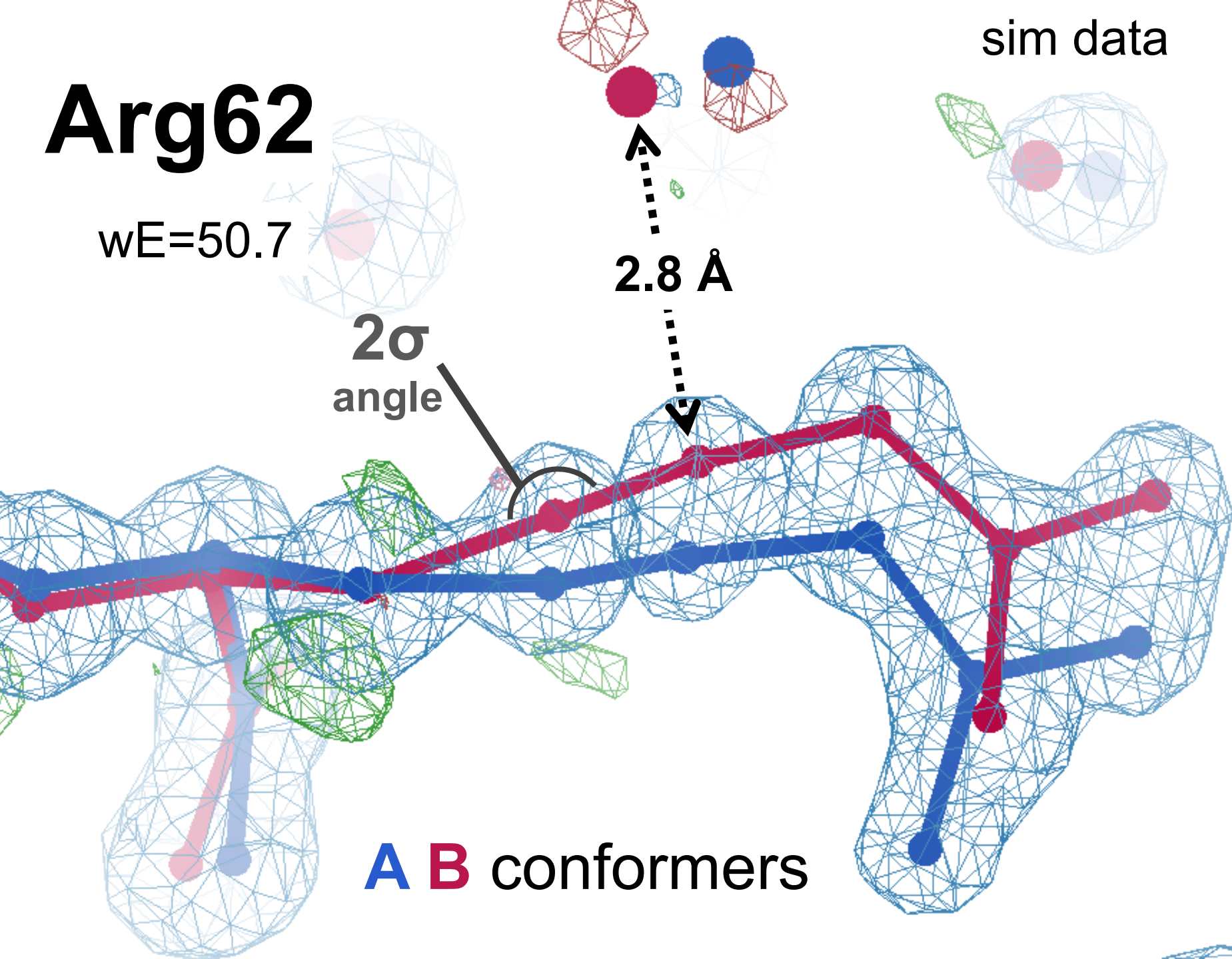
wE=50.7

2σ
angle

2.8 Å

sim data

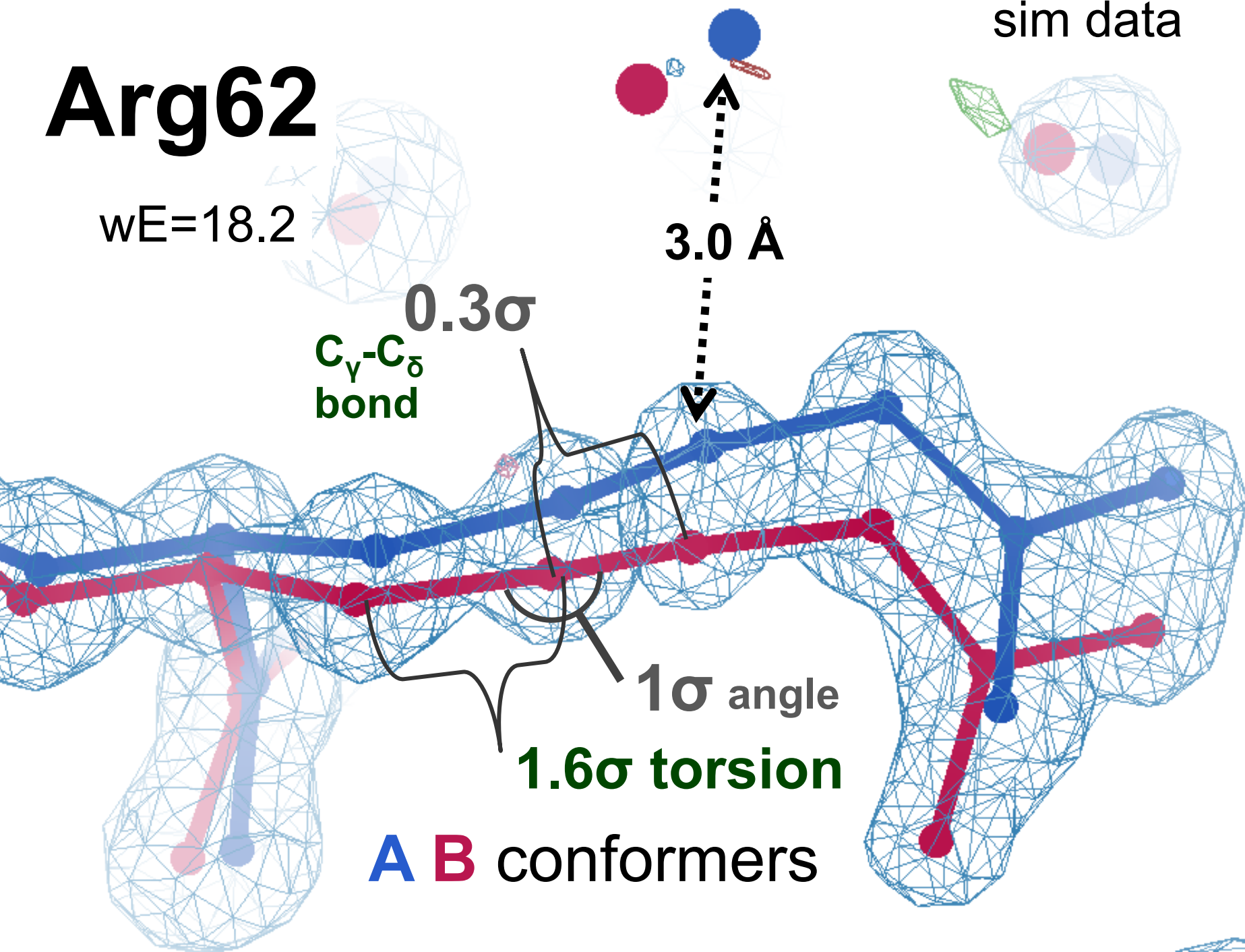
A **B** conformers



Arg62

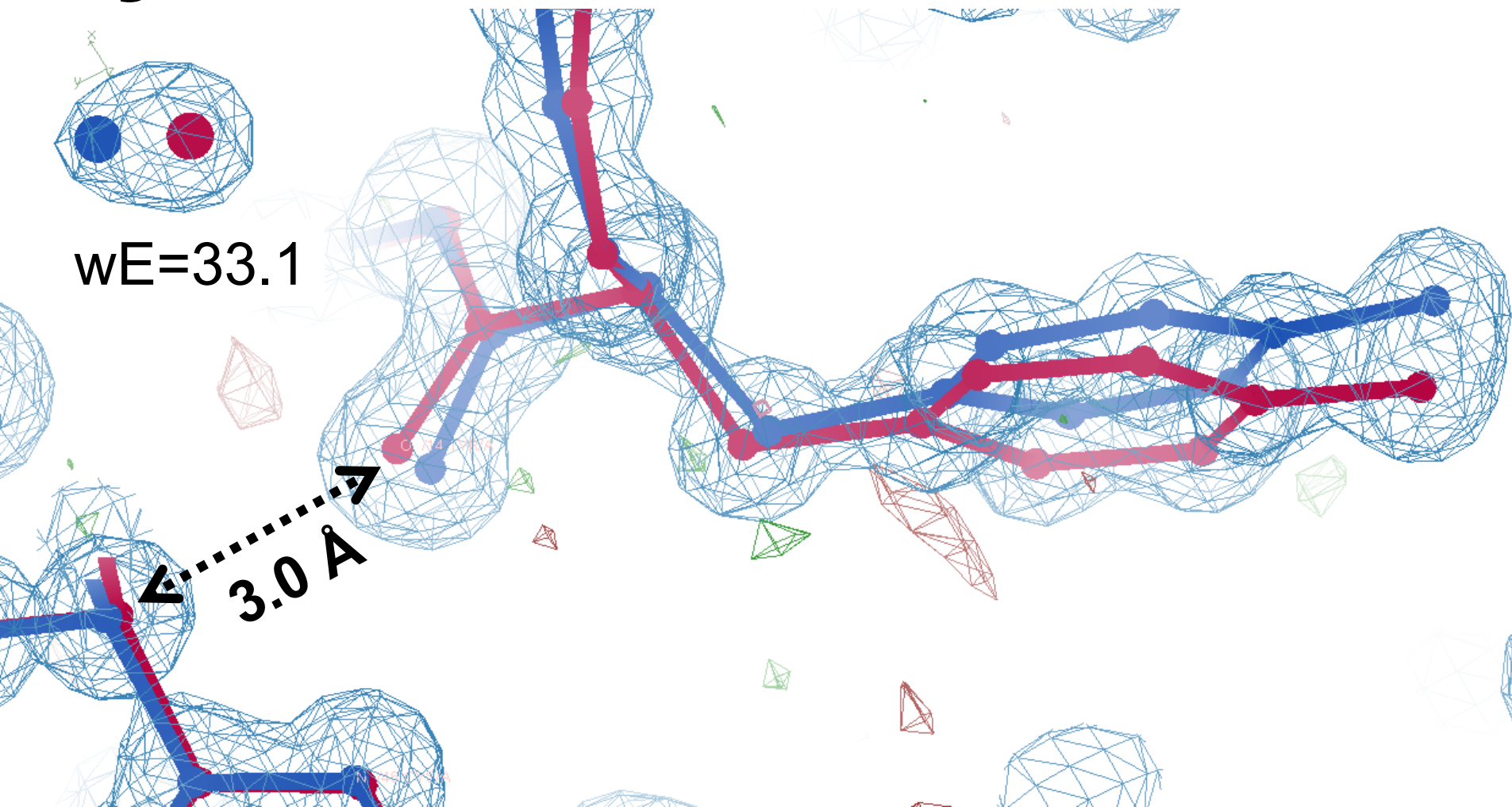
wE=18.2

sim data



Tyr14

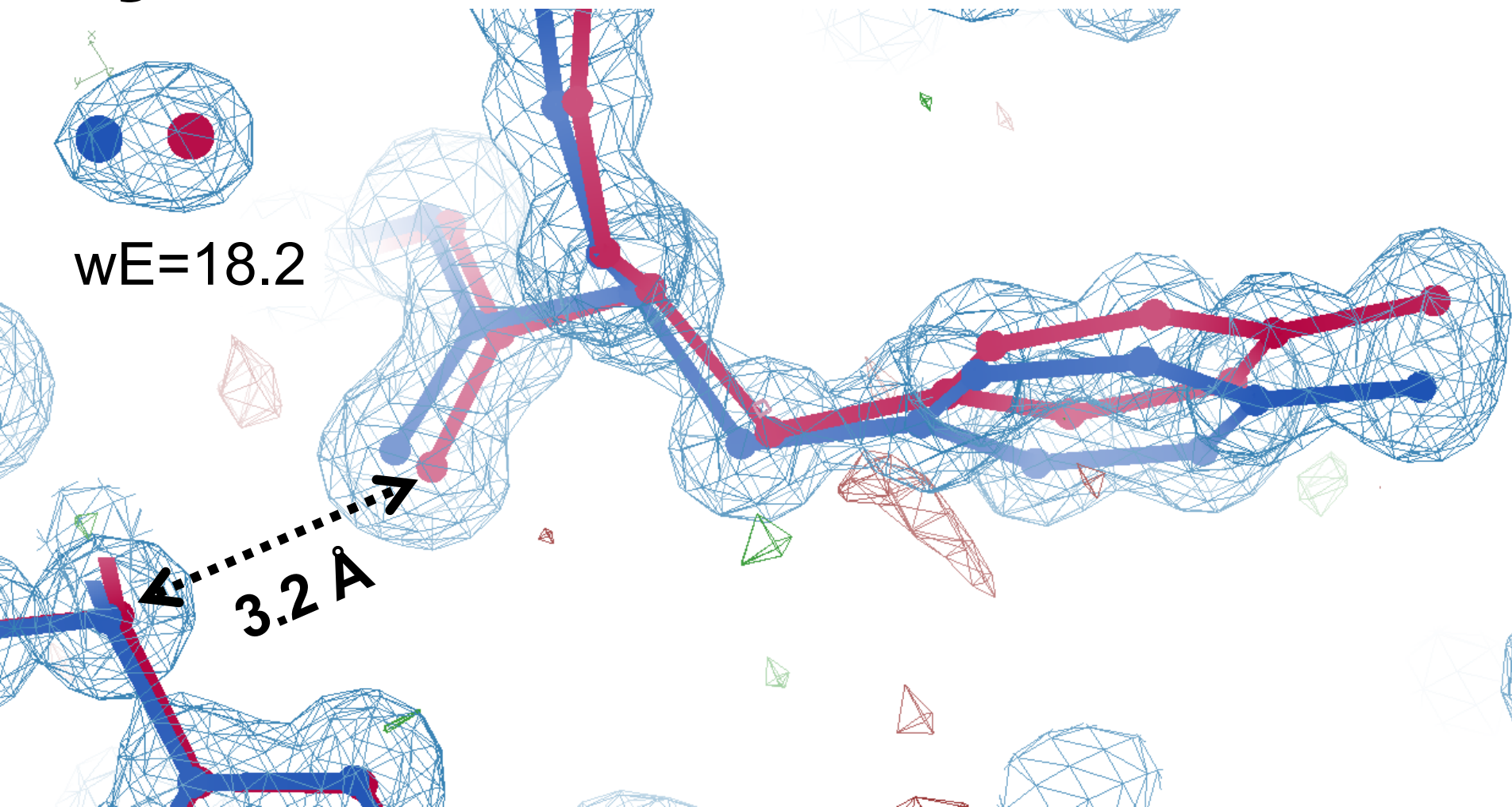
sim data



A B conformers

Tyr14

sim data



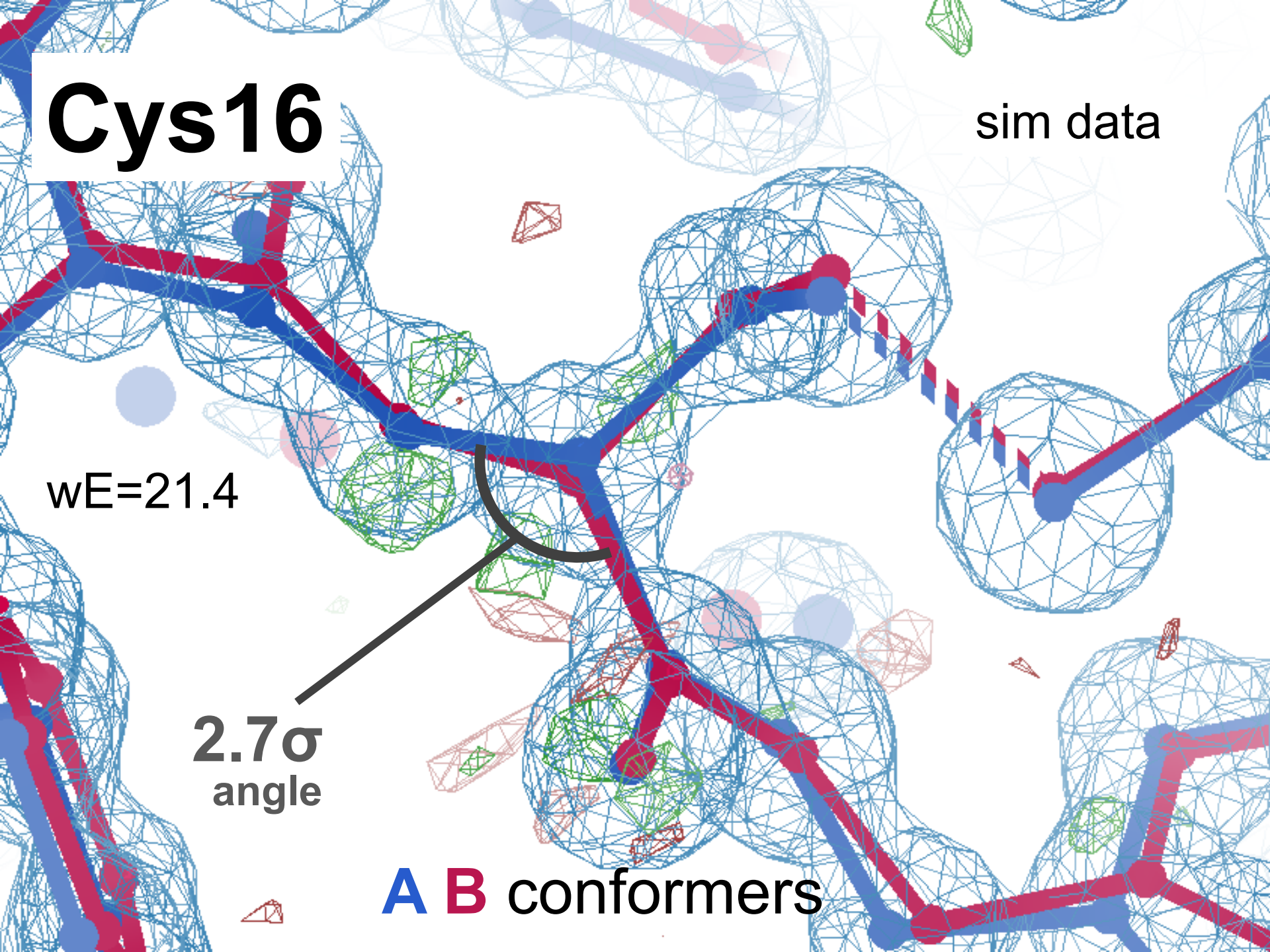
Cys16

sim data

wE=21.4

2.7σ
angle

A **B** conformers



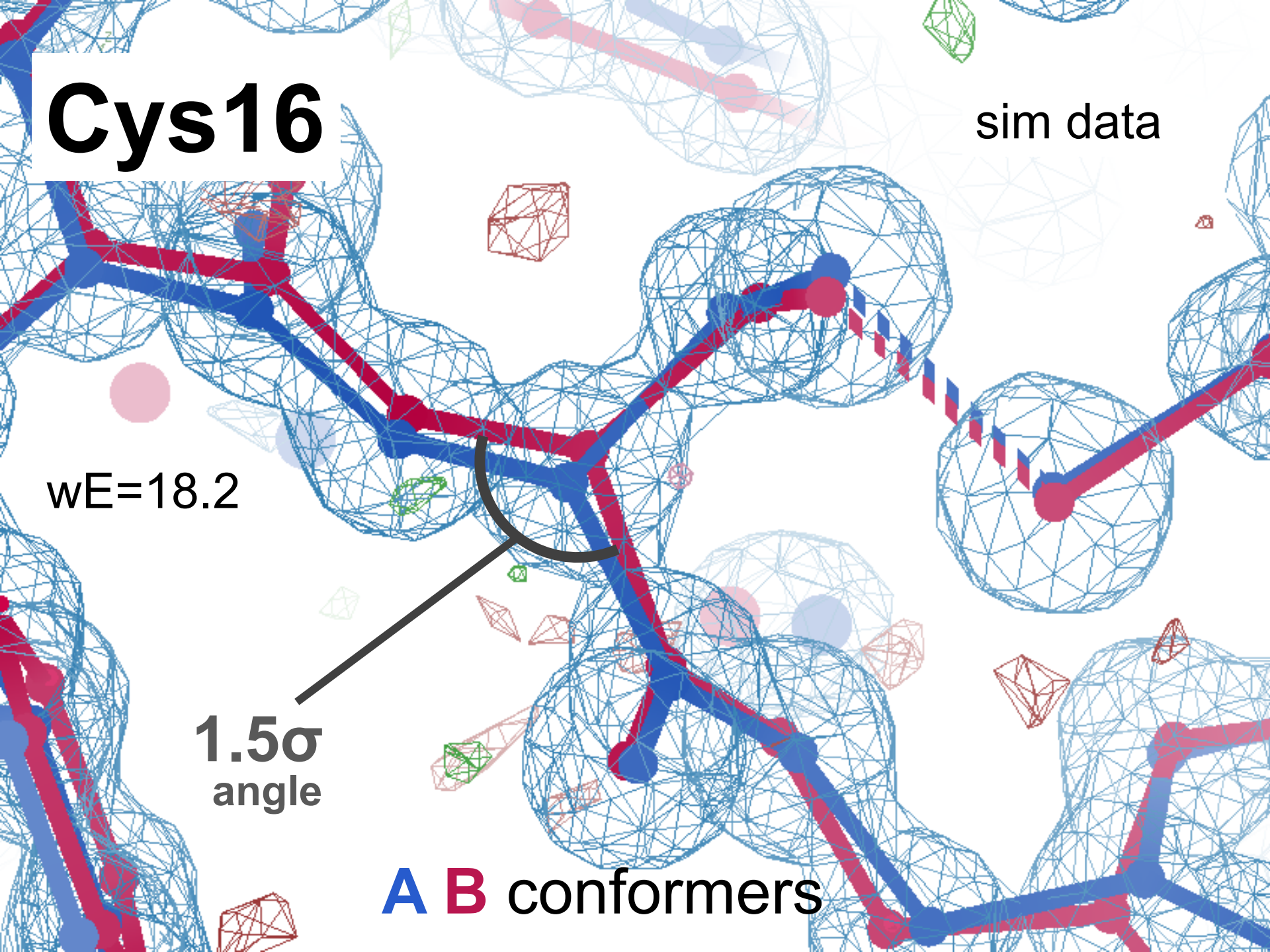
Cys16

sim data

wE=18.2

1.5 σ
angle

A **B** conformers



wE score: key concepts

- Energy $\xleftrightarrow{\text{sqrt()}}$ dev/sigma $\xleftrightarrow{\text{erf()}}$ Probability
- Probability outlier is not noise
 - “clip” outlier energy at “10”
 - Not so sharp transition to outlier
- Tighter Non-bond (Lennard-Jones)

Statistical Potential

$$E = \left(\frac{v - v_0}{\sigma} \right)^2$$

E	“energy”
v	model value
v_0	ideal value
σ	rms deviation expected

Outlier problem: 1 x 6σ $\leftarrow$ 40x 1σ

solution: weight by
“probability its not noise”

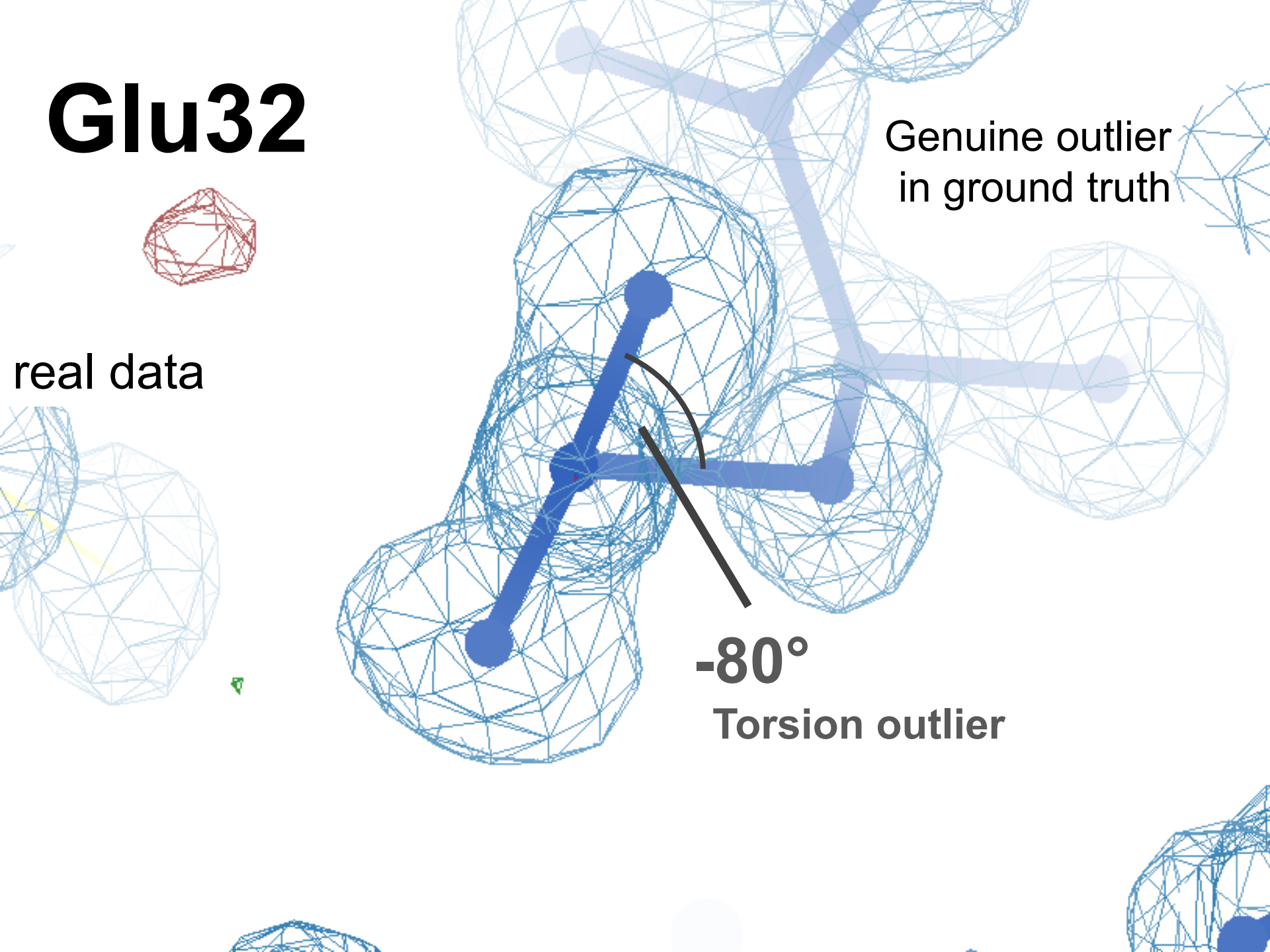
Glu32



real data

Genuine outlier
in ground truth

-80°
Torsion outlier



New Tools!

Tom
Terwilliger



```
phenix.holton_geometry_validation test.pdb
```

```
phenix.create_alt_conf phenix_autobuild.pdb  
refme.mtz \  
nproc=48
```

```
phenix.refine \  
model.pdb refme.mtz \  
main.number_of_mac=10 \  
fit_altlocs_method=masking \  
ordered_solvent=true \  
include_altlocs=true \  
ordered_solvent.mode=every_macro_cycle_after_first \  
refine_oat=true
```

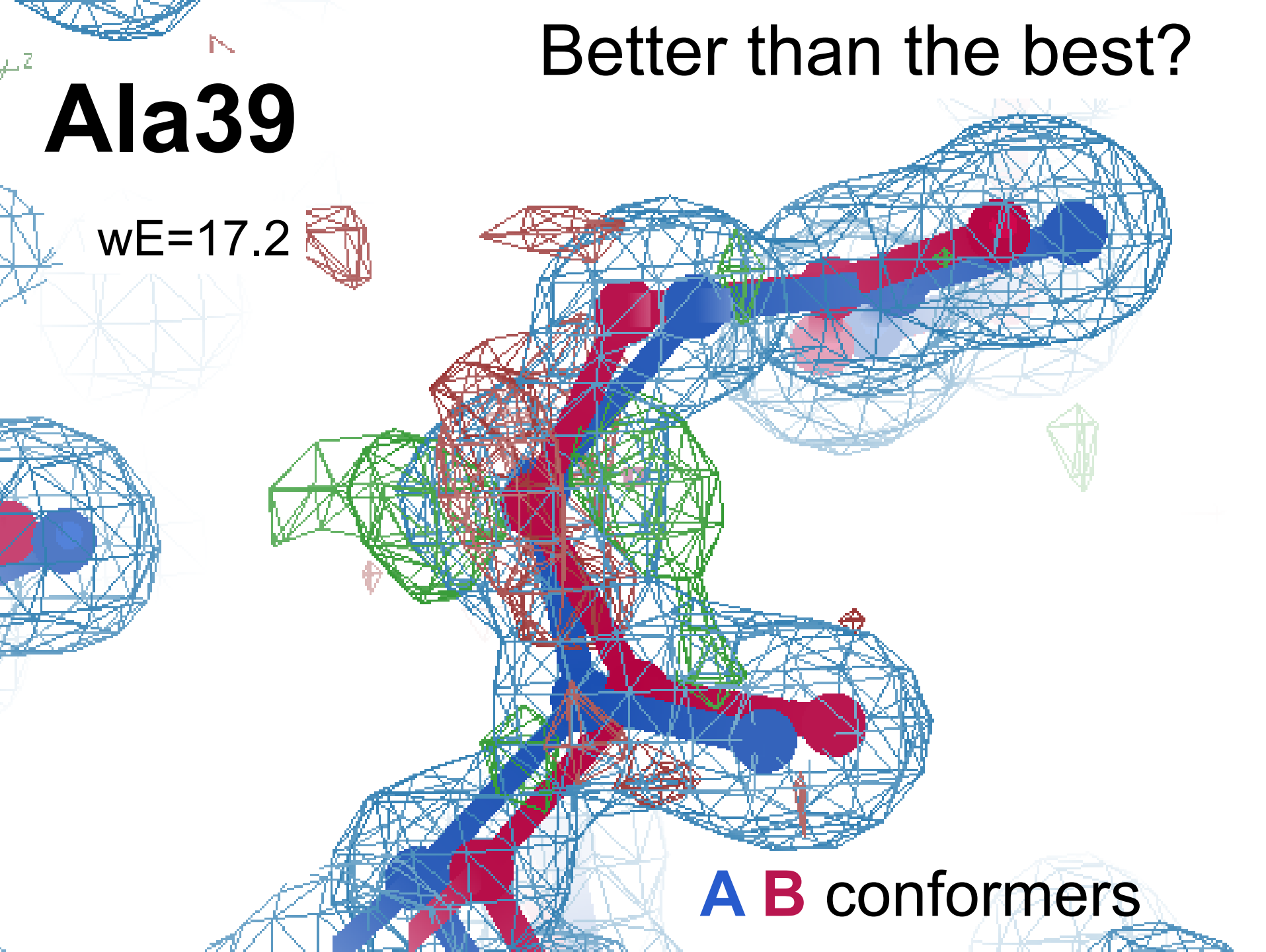
Pavel
Afonine



Better than the best?

Ala39

wE=17.2



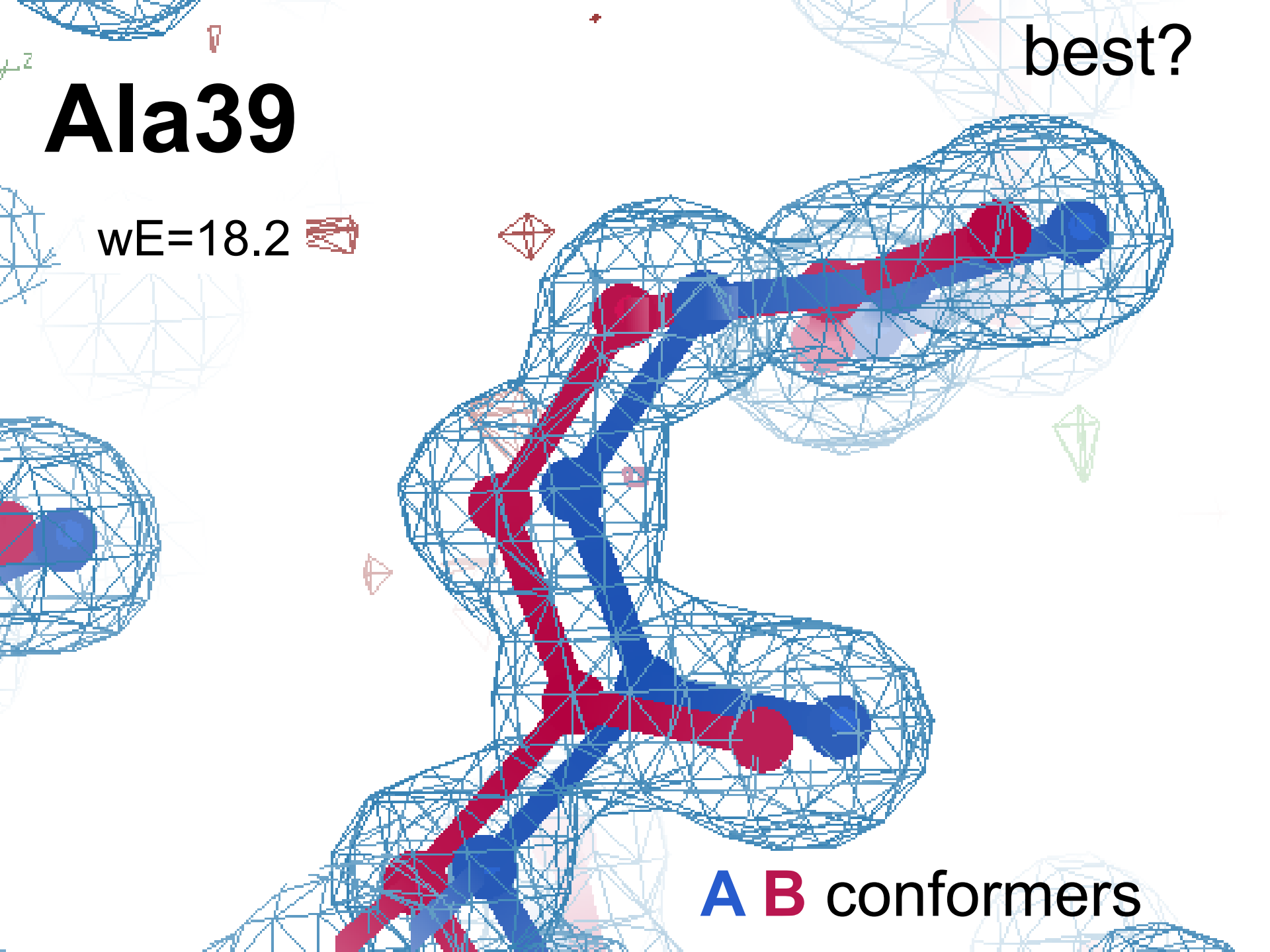
A B conformers

Ala39

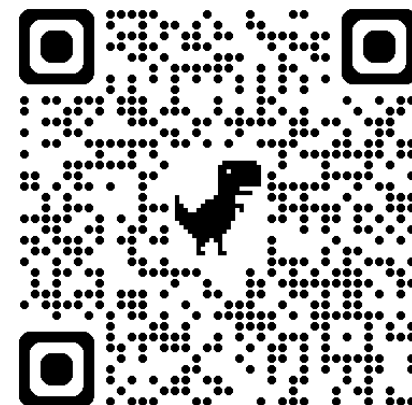
wE=18.2

best?

A **B** conformers



Summary



- $R_{\text{free}} < 3\% \rightarrow$ single e^-
 - Not over-fitting
- Main barrier: tangled ensemble
- Sensible scoring function
 - Probability its not noise
 - some outliers are real
- Recover underlying ensemble
 - Might be required!
- Cooperative motions

\$1000

\$500

verified Score sheet

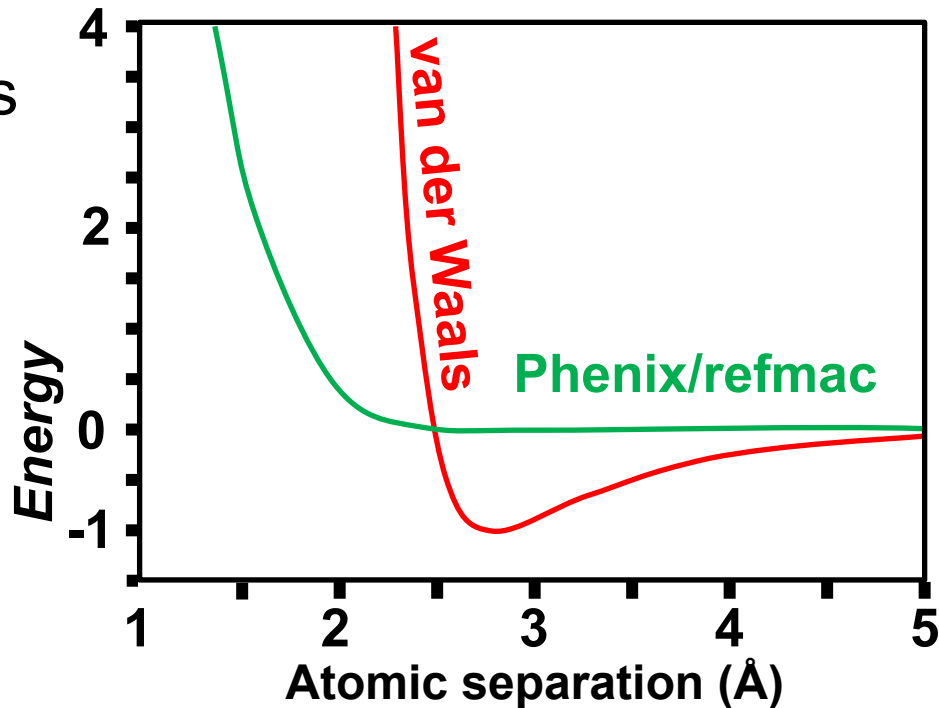
wE	R _{work}	R _{free}	method
185	20.6	21.4	Alphafold2
109.6	8.87	9.44	Phenix.ensemble_refine
97.3	8.84	9.27	qFit best
91.7	3.64	4.27	manual
80.5	4.31	4.75	lotswrong
65.2	6.35	6.93	Amber24
54.6	5.87	6.57	single conf w aniso B
33.5	2.94	3.32	One thing wrong: Ala39
23.5	2.95	3.31	One thing wrong: Val1
21.4	3.12	3.48	Rectified Simulated annealing
18.1	17.9	18.4	Phenix autobuild
18.2	2.79	3.14	best (ground truth)

wE score: key concepts

- **Probability** outlier is not noise
 - “clip” outlier energy at “10”
 - Not so sharp transition to outlier
- Tighter **Non-bond** (Lennard-Jones)

Sensible scoring function

- Statistical potential
 - bonds, angles, planes, torsions, chiral
- Lennard-Jones vdW
 - non-bond and clashes
- Probability $\rightarrow \sigma$ dev
 - Rota, rama
- Peptide bond
 - $\sigma \rightarrow 5^\circ$
- C_β dev
 - $\sigma = 0.05 \text{ \AA}$



Probability that it's not noise

$$P_{nn} = \text{erf}\left(\left|\frac{v - v_0}{\sigma\sqrt{2}}\right|\right)^{N_{\text{things}}}$$

P_{nn} probability
 $v - v_0$ deviation from ideal
 σ rms deviation expected
 $\text{erf}()$ integral of a Gaussian
 N_{things} number of trials

$$\text{erf}(1.0/\sqrt{2}) = 68\% \quad \text{erf}(1.0/\sqrt{2})^{10} = 2\%$$

$$\text{erf}(2.0/\sqrt{2}) = 95\% \quad \text{erf}(2.0/\sqrt{2})^{10} = 63\%$$

$$\text{erf}(4.0/\sqrt{2})^{10,000} = 53\%$$

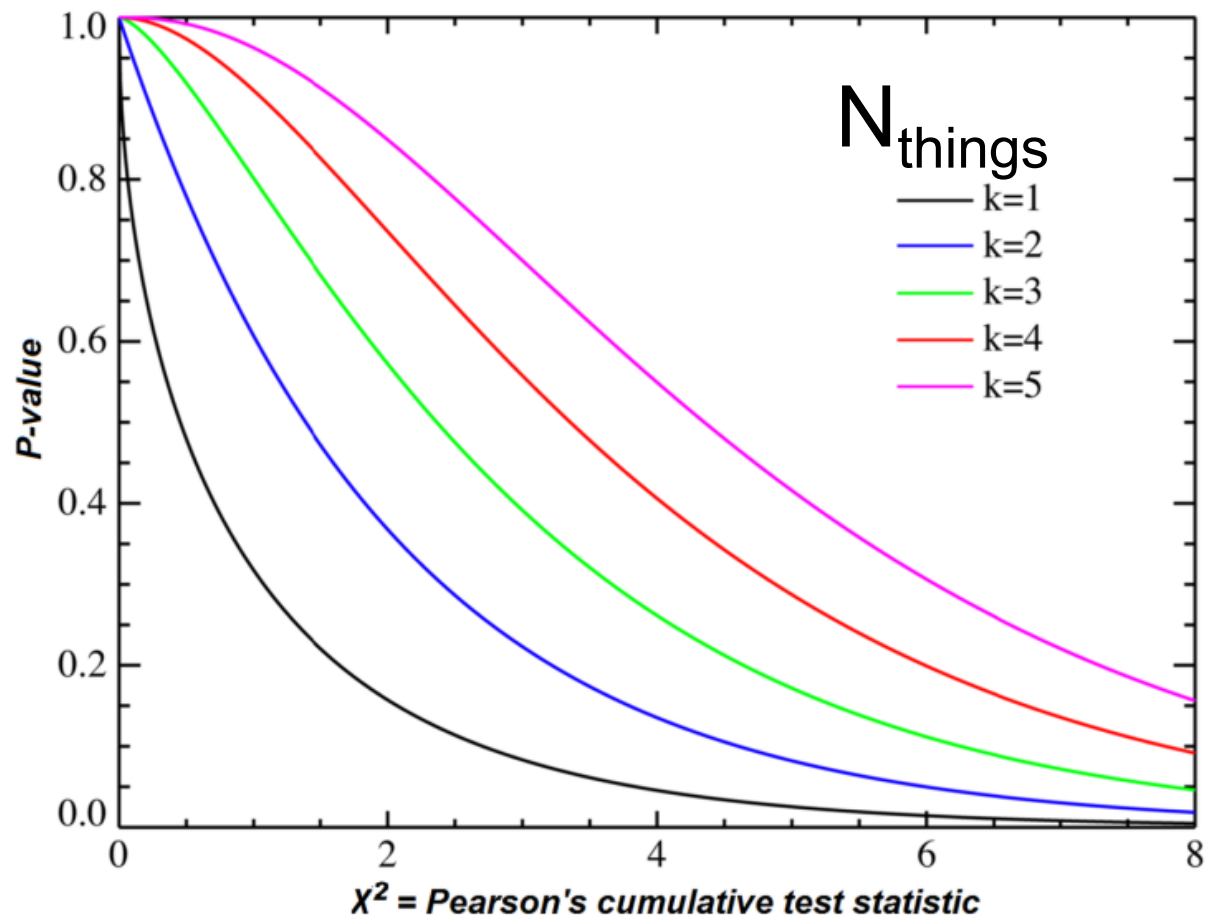
Probability that it's not noise

average/sum of N_{things}

χ^2 test

Probability
That its
Gaussian

tie breaker



“clip” for tolerating true outliers

$$\text{clip}(E) = \begin{cases} E, & \text{if } E < 10 \\ 10 + \log(E) - \log(10) & \end{cases}$$

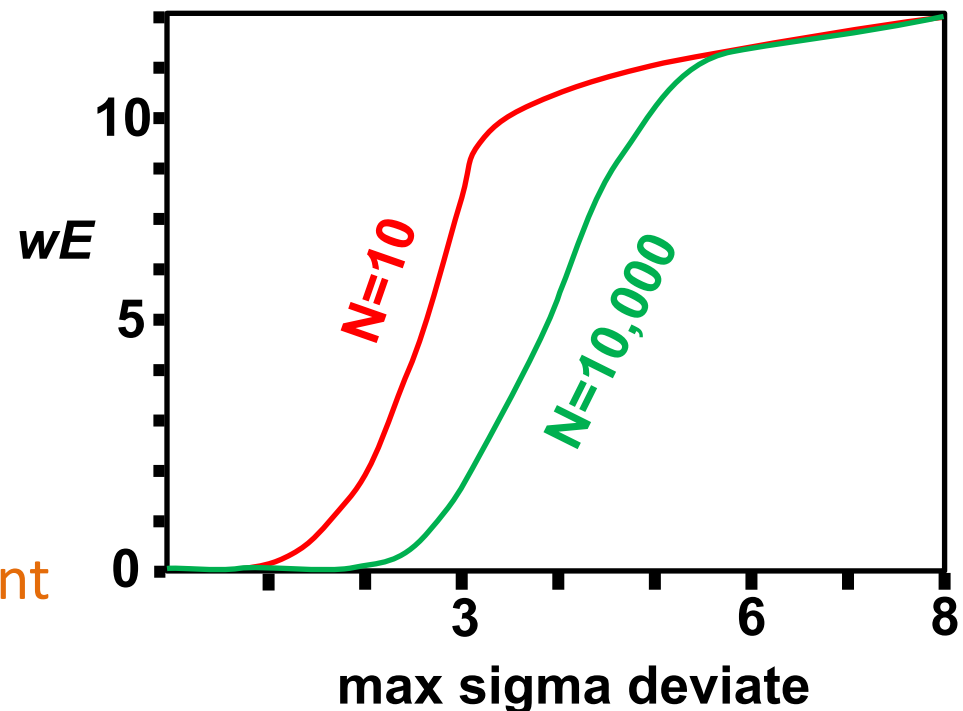
Statistical Energy

$$E = \left(\frac{v - v_0}{\sigma} \right)^2$$

Colloquially:

OK! OK! Its an outlier!
Let's not agonize about it

10 σ vs 10.1 σ **not** more important
than 3.3 σ vs 3.0 σ



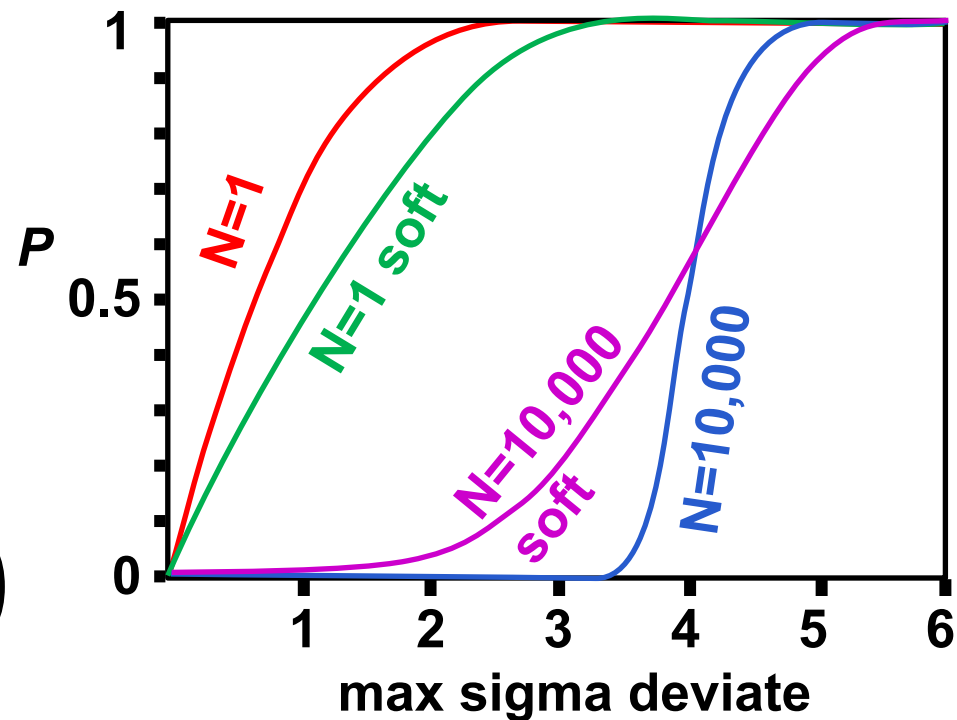
Probability that it's not noise

softer

$$P_{nn}^{soft} = 1 - 2 \left(\left(\frac{|v - v_0|}{\sigma_{P50}} \right)^5 \right)$$

P_{nn} probability
 $v - v_0$ deviation from ideal
 σ rms deviation expected
 $\text{inverf}()$ inverse erf()
 N_{things} number of trials

$$\sigma_{P50} = \sqrt{2} \text{inverf}(0.5^{1/N_{\text{things}}})$$



weighted Energy scoring function

$$wE = \sum_{\text{validation types}} w_{avg} \langle E \rangle + w_{max} \max(\text{clip}(E))$$

`phenix.holton_geometry_validation`

$$w_{max} = P_{nn} \max(\text{clip}(E))$$

$$w_{avg} = \chi^2 \left(\sum_{N_{\text{bonds}}} E \right)$$

$$E = \left(\frac{v - v_0}{\sigma} \right)^2$$

$\max()$ = worst outlier

$$\text{clip}(E) = \begin{cases} E, & \text{if } E < 10 \\ 10 + \log(E) - \log(10) \end{cases}$$

